



### Astrophysical Results from LIGO Scientific Collaboration and Virgo



### GW Data Analysis

- Set Let's play a game
  - www.blackholehunter.org



### Spin-down limit on the Crab pulsar

2 kpc away, formed in a spectacular supernova in 1054 AD

Losing energy in the form of particles and radiation, leading to its spin-down

spin frequency of  $\nu = 29.78 \,\text{Hz}$ spin-down rate,  $\dot{\nu} \approx -3.7 \times 10^{-10} \,\text{Hz}\,\text{s}^{-1}$  $\dot{E} = 4\pi^2 I_{zz} \nu |\dot{\nu}| \approx 4.4 \times 10^{31} \,\text{W}$  $h_0^{\text{sd}} = 8.06 \times 10^{-19} \,I_{38} r_{\text{kpc}}^{-1} (|\dot{\nu}|/\nu)^{1/2}$ 

- We have searched for gravitational waves in data from the fifth science run of LIGO detectors
- The search did not find any gravitational waves

Lack of GW at S5 sensitivity means a limit on ellipticity a factor 4 better than spin-down upper limit - less than 4% of energy in GW
 h<sub>0</sub><sup>95%</sup> = 3.4×10<sup>-25</sup>. ε = 1.8×10<sup>-4</sup>

LSC, ApJ Lett., 683, (2008) 45





### Origin of GRB 070201 from LIGO Observations LSC, Astrophys. J. 681, (2008) 1419

- LSC searched for binary inspirals and did not find any events: results in ApJ 681 1419 2008
- Null inspiral search result
   excludes binary progenitor in
   M31
- Soft Gamma-ray Repeater (SGR) models predict energy release
   <= 10<sup>46</sup> ergs.
- SGR not excluded by GW limits







### Search for GRBs during all of S5

- Nov 2005 Oct 2007: 212 GRBs
- LSC-Virgo searched for 137 GRBs with 2 or more LIGO-Virgo detectors: Null result
- ~25% with redshift, ~10% short duration
- Polarization-averaged antenna response of LIGO-Hanford, dots show location of GRBs during S5-VSRI



### LETTERS

# An upper limit on the stochastic gravitational-wave background of cosmological origin

The LIGO Scientific Collaboration\* & The Virgo Collaboration\*

## Stochastic background

- Metric fluctuations carry energy:
- $\rho_{GW} = \frac{c^2}{32\pi G} < \dot{h}_{ab} \dot{h}^{ab} >$  Characterize by frequency dependence:  $\Omega_{GW}(f) = \frac{1}{\rho_c} \frac{d\rho_{GW}(f)}{d\ln f}$  Describe in terms of strain power spectrum  $S(f) = \frac{3H_0^2}{10\pi^2} \frac{\Omega_{GW}(f)}{f^3}$ • Strain scale:  $h(f) = 6.3 \times 10^{-22} \sqrt{\Omega_{GW}(f)} \left(\frac{100 \text{ Hz}}{f}\right)^{3/2} \text{ Hz}^{-1/2}$

### Searching for a Stochastic Background

$$\Omega_{\rm gw}(f) = \frac{1}{\rho_{\rm crit}} \frac{d\rho_{\rm gw}}{d\ln f}$$

Nucleosynthesis upper-limit

$$\int \frac{df}{f} \Omega_{\rm gw}(f) \lesssim 1.5 \times 10^{-5}.$$

- Upper limit from LIGO data from the 4th Science run  $\Omega_{\rm gw}(f) < 6.5 \times 10^{-5}$
- Data from the 5th science run has improved this better than the nucleosynthesis limit

$$\Omega_{\rm GW} < 6.9 \times 10^{-6}$$



#### LSC, Astrophys. J. 659 (2007) 918





Monday, 4 October 2010

## Astrophysics, Fundamental Physics and Cosmology from GW Observations

B.S. Sathyaprakash Cardiff University, Cardiff, United Kingdom ISAPP School, Pisa, Italy, September 27-29, 2010



### Summary of Sources



### Astrophysics

- Unveiling progenitors of short-hard GRBs
  - Short-hard GRBs are believed to be triggered by merging NS-NS and NS-BH
- Understanding Supernovae
  - Astrophysics of gravitational collapse and accompanying supernova?
- Evolutionary paths of compact binaries
  - Evolution of compact binaries involves complex astrophysics
    - Initial mass function, stellar winds, kicks from supernova, common envelope phase
- Finding why pulsars glitch and magnetars flare
  - What causes sudden excursions in pulsar spin frequencies and what is behind ultra high-energy transients of EM radiation in magnetars
    - Could reveal the composition and structure of neutron star cores
- Ellipticity of neutron stars
  - Mountains of what size can be supported on neutron stars?
- ✤ NS spin frequencies in LMXBs
  - ✤ Why are spin frequencies of neutron stars in low-mass X-ray binaries bounded
- Onset/evolution of relativistic instabilities
  - CFS instability and r-modes

### Supernovae

- Standard candles of astronomy
  - Our knowledge of the expansion rate of the Universe at redshift of z=1 comes from SNe
- Produce dust and affect evolution of galaxies
  - Heavy elements are only produced in SNe
- They are precursors to formation of neutron stars and black holes
  - The most compact objects in the Universe
- SNe cores are laboratories of complex physical phenomena
  - Most branches of physics and astrophysics needed in modelling
    - General relativity, nuclear physics, relativistic magnetohydrodynamics, turbulence, neutrino viscosity and transport, ...
- Insolved problem: what is the mechanism of shock revival?

### Core Collapse SNe



Evolved Massive Star

- Energy reservoir
  - *€* few x 10<sup>53</sup> erg
- Explosion energy
  - **≥** 10<sup>51</sup> erg

- Time frame for explosion
  - ★ 300 1500 ms after bounce
- Formation of black hole
  - · At baryonic mass > 1.8-2.5 M

### Accretion Induced Collapse



White Dwarf (evolved low-mass star)

- Collapse of accreting, probably rotating White Dwarfs
  - Neutrino-driven or magnetorotational explosion
- Explosion probably weak, subluminous

- Might not be seen in optical
- Potential birth site of magnetars - highly (10<sup>15</sup>- 10<sup>16</sup>
   G) magnetized neutron stars

### SNe Rate in ET

- ET sensitive to SNe up to 5 Mpc Could observe one SN once in few years
- Coincident observation with neutrino detectors

Initial LIGO

ET

100

Enhanced LIGO

Advanced LIGO

- Might be allow measurement neutrino masses
- Plots show the spectra of SNe at IO Kpc for two different models

f (Hz)



Monday, 4 October 2010

 $10^{-20}$ 

 $10^{-21}$ 

-22 $10^{-}$ 

 $10^{-23}$ 

10

(at 10 kpc)

 $\mathbf{h}_{\mathrm{char}}$ 

## Neutron Stars

- Great interest in detecting radiation: physics of such stars is poorly understood.
- After 35 years still don't know what makes pulsars pulse or glitch.
- Interior properties not understood: equation of state, superfluidity, superconductivity, solid core, source of magnetic field.
- May not even be neutron stars: could be made of strange matter!



# An extreme challenge



- Neutron star modelling involves the very extremes of physics:
  - Rapid (differential) rotation
  - General relativity
  - **Superfluidity**
  - Strong magnetic fields
  - Crust-core interface
    - Exotic nuclear physics
    - Strange quarks, hyperons

### **Pulsar Glitches**

- Pulsars have fairly stable rotation rates:
  - However, observe the secular increase in pulse period
- Slitches are sudden dips in the rotation period
  - Vela shows glitches once every few years
- Could be the result of transfer of angular momentum from core to crust
  - At some critical lag rotation rate superfluid core couples to the curst imparting energy to the crust

 $\Delta E = \Delta J \Omega_{\text{lag}}$  $\Delta J \sim I_* \Delta \Omega$  $\Delta\Omega/\Omega \sim 10^{-6}$  $\Delta E \sim 10^{-13} \text{--} 10^{-11} \text{M}_{\odot} c^2$ 





ΙΛ

### NS Normal Mode Oscillations

- Sudden jolt due to a glitch, and superfluid vortex unpinning, could cause oscillations of the core, emitting gravitational waves
  - These normal mode oscillations have characteristic frequencies and damping times that depend on the equation-of-state
- Detecting and measuring normal modes could reveal the equation-of-state of neutron stars and their internal structure



### Accreting Neutron Stars

- Spin frequencies of accreting NS seems to be stalled below 700 Hz
  - Well below the break-up speed
- What could be the reason for this stall?
  - Balance of accretion torque with GW back reaction torque
- Could be explained if ellipticity is ~ 10<sup>-8</sup>
  - Could be induced by mountains or relativistic instabilities, e.g. r-modes





#### pulses & burst oscillations

### Sensitivity to Accreting NS



### **GRB** Progenitors

- Intense flashes of gammarays:
  - Most luminous EM source since the Big Bang
  - X-ray, UV and optical afterglows
- Bimodal distribution of durations
  - Short GRBs
    - $\therefore$  Duration: T<sub>90</sub> < 2 s
    - · Mean redshift of 0.5
  - ✤ Long GRBs
    - $\therefore$  Duration T<sub>90</sub> > 2 s
    - ↔ Higher z, track Star Form. Rate.



- Long GRBs
  - Core-collapse SNe, GW emission not well understood
    - Could emit burst of GW
- Short GRBs
  - Could be the end state of the evolution of compact binaries
    - ·⊱ BNS, NS-BH

#### GRBs in ET

- Short-hard GRBs might be detectable at redshift z=2
- An ET network could measure the binary orientation, masses, spins, and help build better models
- Should be possible to shed light on GRB progenitors

#### Gamma-Ray Bursts (GRBs): The Long and Short of It



## Astrophysics

- What is the population of white dwarfs in our galaxy?
  - What is their mass function, are there white dwarfs that are very close to Chandrasekhar limit?
- Do massive black hole mergers produce detectable EM afterglows?
- At what rate do massive black holes form and merger throughout the Universe?
  - How does this rate evolve with red-shift?
- How frequently do intermediate and stellar-mass black holes infall into massive black holes?
  - What is the merger history of massive black holes at galactic nuclei

## White Dwarf Binaries and AM CVn Systems in LISA





## Black hole seeds

# How to supermassive black holes form and evolve?

# Are black holes the end state of gravitational collapse?

### Is no-hair theorem valid?

### Sagittarius A: A Galactic SMBH





### Super-massive black hole mergers



### SMBH binary in NGC 6240

#### NGC6240, Kamossa et al



- X-ray observations have revealed that the nucleus of NGC 6240 contains an SMBH binary that will coalesce within the Hubble time
- The high visibility of the signal means we can see SMBH binaries anywhere in the Universe
- We can catch the signal at early times to predict the precise time and position of the coalescence event, allowing the event to be observed simultaneously by other telescopes.



### Visibility of SMBH binary mergers



## Massive black holes in LISA

- When and where do supermassive black holes form and grow?
- What is the mass function of supermassive black holes?
- What can we find in the environment around black holes?
  - Population of smaller black holes, neutron stars, white dwarfs?

### Models of Black Hole Seeds and Their Evolution

Class. Quantum Grav. 26 (2009) 094027

K G Arun et al



### Expected Detection of SMBBH Mergers in LISA

Numbers for the 6-link model are followed, within parenthesis, by those for the baseline (i.e., 4-link) LISA noise model



LISA should detect and verify the nature of black hole seeds

Class. Quantum Grav. 26 (2009) 094027

K G Arun et al

Model	N	N <sub>det</sub>	$N_{10\%D_{\rm L}}$	$N_{10{ m deg}^2}$	$N_{10\mathrm{deg}^2,10\%D_\mathrm{L}}$	$N_{1 deg^2}$	$N_{1 deg^2, 1\% D_L}$
SE	80	33 (25)	21 (8.0)	8.2 (1.5)	7.9 (1.1)	2.2 (0.6)	1.7 (0.1)
SC	75	34 (27)	17 (4.4)	6.1 (0.4)	5.5 (0.4)	1.3 (0.1)	1.3 (0.1)
LE	24	23 (22)	21 (7.7)	10 (0.8)	10 (0.7)	2.2 (0.1)	1.2 (0.05)
LC	22	21 (19)	14 (4.3)	6.5 (0.5)	5.4 (0.5)	1.8 (0.04)	1.0 (0.1)


### Mass reach of LISA

RWF=Restricted Waveform:FWF=Full Waveform:all harmonicsonly the dominant harmonicup to 7 times the orbital frequency



### LISA's ability in measuring the Source

- Because of LISA's superb visibility to supermassive black holes the parameters of the binary can be measured to phenomenal accuracy: The parameters we are interested in are:
  - The epoch when the binary merges, chirpmass and reduced mass of the binary, spinparameters, the sky location, luminosity distance, orientation of the binary with respect to the line of sight.

### Parameter measurement distributions

 $(10^{6}, 10^{6}) M_{\odot}$ 



### Parameter measurement distributions





### Parameter measurement distributions





### Capture of Small Black Holes by Intermediate-Mass Black Holes



### Testing the No-Hair Theorem

### Image: AEI/Einstein Online

Ryan

### Testing the No-Hair Theorem

### Image: AEI/Einstein Online

Ryan

### Gravitational Capture and Testing Uniqueness of Black Hole Space-times



# Black hole quasi-normal modes

- Damped sinusoids with characteristic frequencies and decay times
  - In general relativity frequencies  $f_{lmn}$  and decay times  $t_{lmn}$  all depend only on the mass M and spin q of the black hole
- Measuring two or modes unambiguously, would severely constrain general relativity
  - If modes depend on other parameters (e.g., the structure of the central object), then test of the consistency between different mode frequencies and damping times would fail
- LISA should be able to observe formation of black holes out to red-shifts of several









# Cosmology

- Cosmography
  - Hubble parameter, dark matter and dark energy densities, dark energy EoS w, variation of w with z
- Black hole seeds
  - Black hole seeds could be intermediate mass BH
  - ✤ Hierarchical growth of central engines of BH
- Dipole anisotropy in the Hubble parameter
  - The Hubble parameter will be "slightly" different in different directions due to the local flow of the Milkyway
- Anisotropic cosmologies
  - In an anisotropic Universe the distribution of H on the sky should show residual quadrupole and higher-order anisotropies
- Primordial gravitational waves
  - Quantum fluctuations in the early Universe could produce a stochastic b/g
- Production of GW during early Universe phase transitions
  - Phase transitions, pre-heating, re-heating, etc., could produce detectable stochastic GW

# Cosmological parameters

★ Luminosity distance Vs. red shift depends on a number of cosmological parameters  $H_0$ ,  $Ω_M$ ,  $Ω_b$ ,  $Ω_\Lambda$ , w, etc.

$$D_L(z) = \frac{c(1+z)}{H_0} \int_0^z \frac{dz}{\left[\Omega_M(1+z)^3 + \Omega_\Lambda(1+z)^{3(1+w)}\right]^{1/2}}$$

- Einstein Telescope will detect 1000's of compact binary mergers for which the source can be identified (e.g. GRB) and red-shift measured.
- A fit to such observations can determine the cosmological parameters to better than a few percent.

#### Schutz 86 **Compact Binaries are Standard Sirens**

- Amplitude of gravitational waves depends on  $h \propto \frac{\mathcal{M}^{5/6}}{D_r}$  Chirp-mass= $\mu^{3/5}M^{2/5}$
- Gravitational wave observations can measure both
  - Amplitude (this is the strain caused in our detector)
  - Chirp-mass (because the chirp rate depends on the chirp mass)
- Therefore, binary black hole inspirals are standard sirens
  - From the apparent luminosity (the strain) we can conclude the luminosity distance
- However, GW observations alone cannot determine the red-shift to a source
- Ioint gravitational-wave and optical observations can facilitate a new cosmological tool

### ET and Cosmology

### SNR in ET for coalescences at z=0.5





Measurement of DM, DE, w



Measurement of DM and w



Measurement of w



### Measuring Dark Energy and Dark Matter



# LISA's ability to measure cosmological parameters

#### K.G. ARUN et al.

PHYSICAL REVIEW D 76, 104016 (2007)

# Measuring w with LISA

$\frac{\Delta \ln D_{\rm L}}{(10^{-2})}$	$\frac{\Delta\Omega_{\rm S}}{(10^{-6}~{\rm str})}$	$\frac{\Delta \ln \mathcal{M}}{(10^{-6})}$	$\Delta\delta$ (10 <sup>-6</sup> )	$\Delta t_{\rm C}$ (sec)	<b>N</b> <sub>clusters</sub>	$\Delta w$
1.2	12	6.0	31	1.7	0.25	0.068
0.88	4.3	4.6	23	1.2	0.088	0.050
1.1	110	4.7	21	1.7	2.2	0.062
0.58	13	3.5	16	1.1	0.27	0.033
0.25	170	3.3	12	2.6	3.5	• • •
0.17	26	2.7	9.7	1.1	0.53	0.0096
0.74	150	3.1	15	1.2	3.1	• • •
0.19	13	2.5	12	0.58	0.27	0.011
15	84	2.3	8.0	2.1	1.7	0.82
0.11	8.1	1.7	7.9	0.69	0.17	0.0062
0.42	220	3.9	15	2.9	4.5	• • •
0.24	65	3.0	11	1.6	1.3	0.014
0.58	410	3.5	13	1.1	8.4	• • •
0.45	300	2.9	10	0.74	6.1	• • •
		$(m_1, m_2)$	$=(10^5,$	$10^6)M_{\odot}$		

#### K.G. ARUN et al.

# A lighter system

$\frac{\Delta \ln D_{\rm L}}{(10^{-2})}$	$\frac{\Delta\Omega_{\rm S}}{(10^{-6} \text{ str})}$	$\frac{\Delta \ln \mathcal{M}}{(10^{-6})}$	$\Delta\delta$ (10 <sup>-6</sup> )	$\Delta t_{\rm C}$ (sec)	<b>N</b> <sub>clusters</sub>	$\Delta w$			
1.3	21	5.5	13	3.2	0.43	0.073			
1.0	8.4	4.2	9.1	2.1	0.17	0.056			
1.1	120	4.2	9.2	2.5	2.4	0.062			
0.70	25	3.3	6.5	1.7	0.51	0.039			
0.33	170	3.4	5.8	2.7	3.5	• • •			
0.25	53	2.6	4.2	1.6	1.1	0.014			
0.78	160	3.0	6.8	1.7	3.3	• • •			
0.26	27	2.3	5.0	1.0	0.55	0.015			
15	87	2.4	3.8	2.2	1.8	1.0			
0.19	25	2.0	3.9	1.3	0.51	0.011			
0.47	240	4.1	7.2	3.1	4.9	• • •			
0.32	110	2.9	4.8	2.1	2.2	0.018			
0.57	420	3.1	6.1	1.6	8.6	• • •			
0.50	350	2.5	4.2	1.1	7.1	• • •			
$(m_1, m_2) = (6.45 \times 10^4, 1.29 \times 10^6) M_{\odot}$									

# Spin-Precession: More accurate Luminosity Distance Measurement



# Spin-Precession: Improvement in Dark Energy Measurement



## **Fundamental Physics**

#### Properties of gravitational waves

- Testing the wave generation formula beyond the quadrupole formula
  - Binary pulsars consistent with quadrupole formula but they cannot measure the properties of GW
- How many polarizations?
  - In Einstein's theory only two polarizations; a scalar-tensor theory could have six
- Do gravitational waves travel at the speed of light?
  - \* There are strong motivations from string theory to consider massive gravitons

#### EoS of dark energy

- GW from inspiralling binaries are standard sirens
- EoS of supra-nuclear matter
  - Signature of EoS in GW emitted when neutron stars merge
- Black hole no-hair theorem and cosmic censorship
  - Are BH (candidates) of nature BH of general relativity?
- Merger dynamics of spinning black hole binaries

# Do gravitational waves travel at the speed of light?

- Coincident observation of a supermassive black hole binary and the associated gravitational radiation can be used to constrain the speed of gravitational waves:
- If  $\Delta t$  is the time difference in the arrival times of GW and EM radiation and D is the distance to the source then the fractional difference in the speeds is

$$\frac{\Delta v}{c} = \frac{\Delta t}{D/c} \simeq 10^{-14} \left(\frac{\Delta t}{1 \text{sec}}\right) \left(\frac{D}{1 \text{Mpc}}\right)$$

 Can be used to set limits on the mass of the graviton no strong motivation for massive graviton theory due to vDVZ discontinuity, but might be avoided

Will (1994, 98)

# Massive Graviton: Dispersion as Waves Propagate

A massive graviton induces dispersion in the waves

$$hf \gg m_{\rm g}c^2$$
  $\frac{v_{\rm g}^2}{c^2} = 1 - \frac{m_{\rm g}^2 c^4}{E^2},$ 

 $v_{\rm g}/c \approx 1 - \frac{1}{2} (c/\lambda_{\rm g} f)^2$ , where  $\lambda_{\rm g} = h/m_{\rm g} c$ 

 Arrival times are altered due to a massive graviton frequency-dependent effect

$$t_a = (1+Z) \left[ t_e + \frac{D}{2\lambda_g^2 f_e^2} \right]$$

Will (1994, 98)

# Bound on $\lambda_g$ as a function of total mass

Limits based on GW observations will be five orders-ofmagnitude better than solar system limits

$$V(r) = \frac{GM}{r} \exp(-r/\lambda_{\rm g})$$
$$\lambda_{\rm g} > 2.8 \times 10^{12} \text{ km}$$

✤ Still not as good as (model-dependent) limits based on dynamics of galaxy clusters  $\lambda_g > 6 \times 10^{19}$  km



Berti, Buonanno and Will (2006)

#### Arun and Will (2009)



# Counting the Polarization States Only two states in GR: $h_+$ and $h_x$

Gravity's Standard Sirens

# Counting the Polarization States Only two states in GR: $h_{+}$ and $h_{*}$





#### Plus polarization

**Cross polarization** 

Gravity's Standard Sirens
## Polarization States in a Scalar-Tensor Theory

- Polarization tests are qualitative tests
- A single measurement is good enough to rule the theory out
- In Einstein's theory there are only two polarization states - the plus and the cross polarizations
- In a scalar-tensor theory of gravity, there are six different polarization modes

Cliff Will, Living Rev. in Relativity



Today 14 billion years Life on earth A brief history Acceleration 11 billion years Dark energy dominate Solar system forms Star formation peak the Universe Galaxy formation era Earliest visible galaxies 700 million year Recombination Atoms form 400,000 years CMB  $f < 3 \times 10^{-17} h$ Hz probes 300,000yrs  $< t_e < 14$  Gyrs Relic radiation decouples (CMB) Matter domination 5,000 years Onset of gravitational collapse Nucleosynthesis Light elements created - D, He, Li Nuclear fusion begins Pulsars  $f \sim 10^{-8}$ Hz probe  $t_e \sim 10^{-4}$ s ( $T \sim 50$ MeV) Ouark-hadron transition Protons and neutrons formed Electroweak transition LISA  $f \sim 10^{-3}$ Hz probes  $t_e \sim 10^{-14}$ s ( $T \sim 10$ TeV) Electromagnetic and weak nuclear forces first differentiate ET  $f \sim 10$  Hz probes  $t_{e} \sim 10^{-20}$  s ( $T \sim 10^{6}$  GeV) Supersymmetry breaking Axions etc.? LIGO  $f \sim 100 \text{ Hz}$  probes  $t_e \sim 10^{-24} \text{s} (T \sim 10^8 \text{GeV})$ Grand unification transition Electroweak and strong nuclear forces differentiate Inflation (Planck scale  $f \sim 10^{11}$ Hz has  $t_e \sim 10^{-43}$ s ( $T \sim 10^{19}$ GeV) Quantum gravity wall Spacetime description breaks down

Slide from Shellard

## Monday, 4 October 2010

## Landscape of Stochastic GW in ET



Monday, 4 October 2010

## What can gravitational waves reveal about the Universe?

- Was Einstein right?
  - Is the nature of gravitational radiation as predicted by Einstein?
  - Are black holes in nature black holes of GR?
  - Are there naked singularities?
- Unsolved problems in astrophysics
  - What is the origin of gamma ray bursts?
  - What is the structure of neutron stars and other compact objects?
- Cosmology
  - How did massive black holes at galactic nuclei form and evolve?
  - Were there phase transitions in the early Universe?
- Fundamental questions
  - ★ What were the physical conditions at the big bang?
  - What is dark energy?
  - Are there really ten spatial dimensions?