

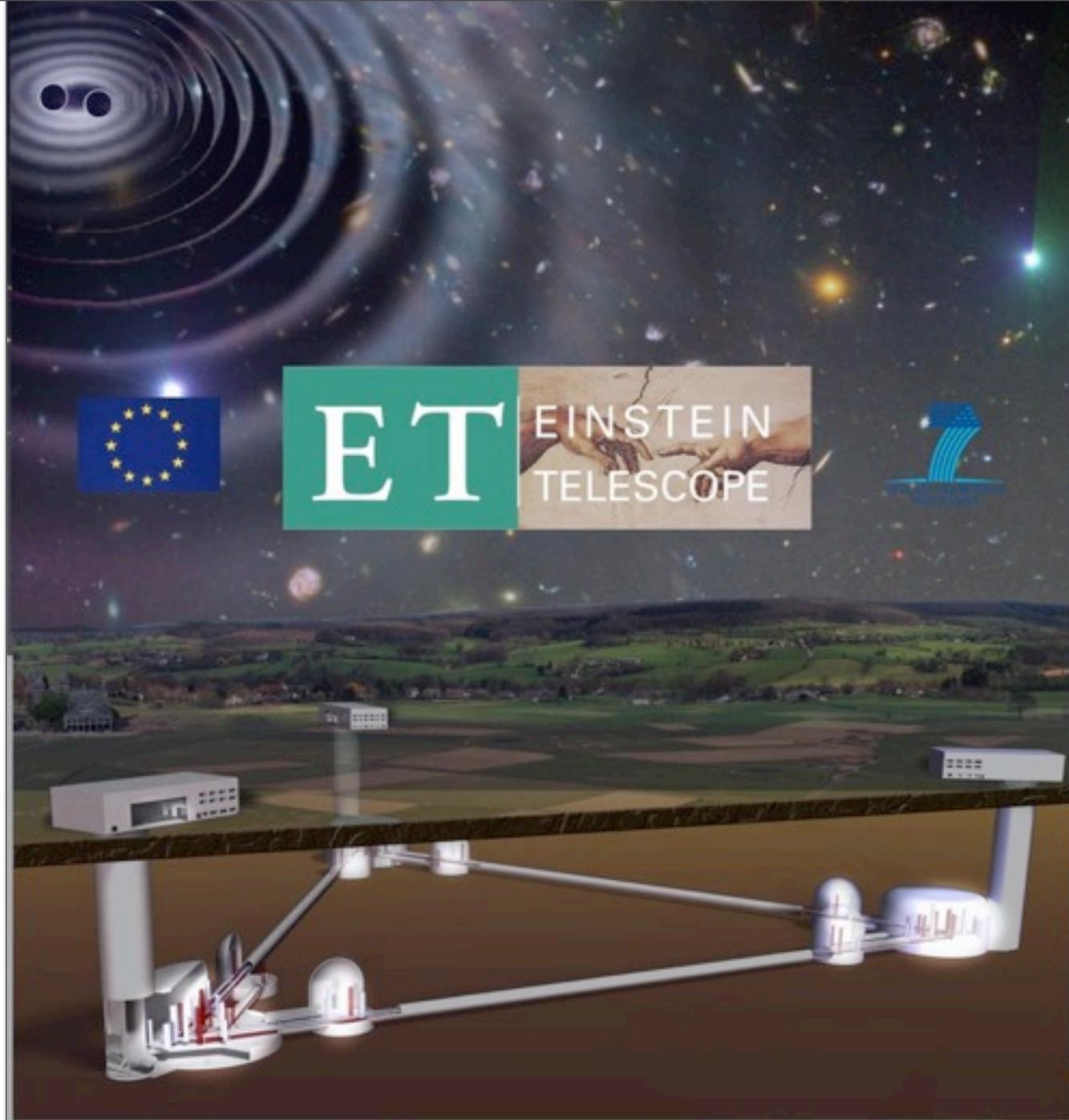
# Einstein Telescope: The Science Case

EGO, Cascina, Italy, May 20 2011

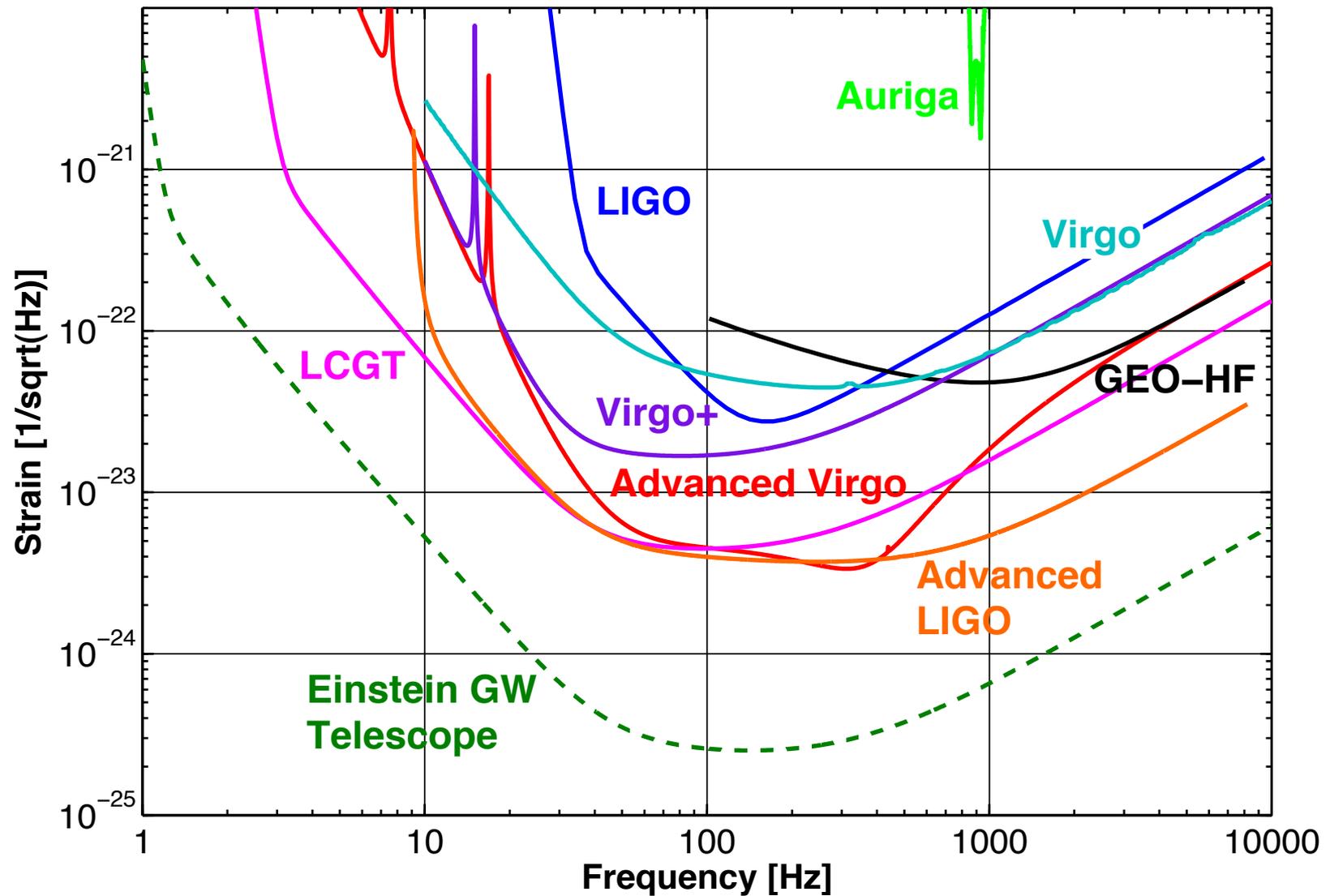
B.S. Sathyaprakash

School of Physics and Astronomy, Cardiff University, UK  
on behalf of the Einstein Telescope Design Study Team





# Expected ET Sensitivity



# What will ET observe and what can it tell?

- ET will observe radiation arising from
  - black hole collisions when the Universe was still in its infancy assembling the first galaxies
  - neutron star collisions when star formation in the Universe was at its peak
  - formation of black holes and neutron stars in supernovae and collapsars in the local neighbourhood
  - stochastic backgrounds of cosmological and astrophysical origin
- ET will provide new insights into
  - the secret births and lives of black holes and neutron stars, their demographics, populations and their masses and spins
  - dark energy and its variation with redshift
  - equation of state of matter at supra-nuclear densities
  - early history of the Universe's evolution

# Compact binaries for fundamental physics, cosmology and astrophysics

- Black holes and neutron stars are the most compact objects
- The potential energy of a test particle is equal to its rest mass energy

$$\frac{GmM}{R} \sim mc^2$$

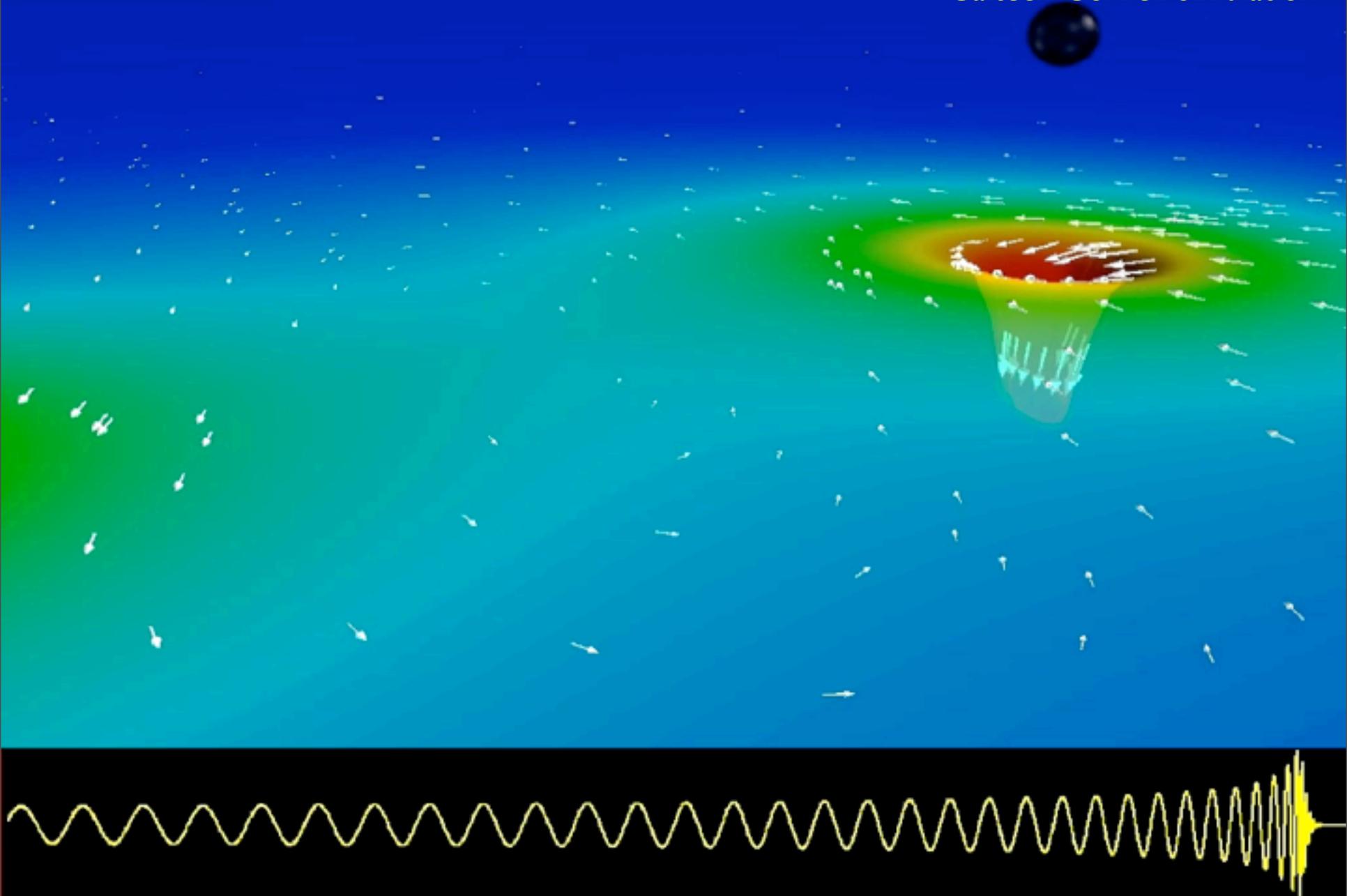
- Being the most compact objects, they are also the most luminous sources of gravitational radiation
- The luminosity of a neutron star binary increases a **billion** times in the course of its evolution through a ET's sensitivity band
- The GW luminosity of a binary black hole **outshines**, during merger, the EM luminosity of **all the stars** in the Universe
- Compact binaries are **self-calibrating** standard sirens
- GW observations measure both the apparent luminosity (strain) and absolute luminosity (chirp rate) of a source

# Numerical Simulation of Merging Black Hole Binaries

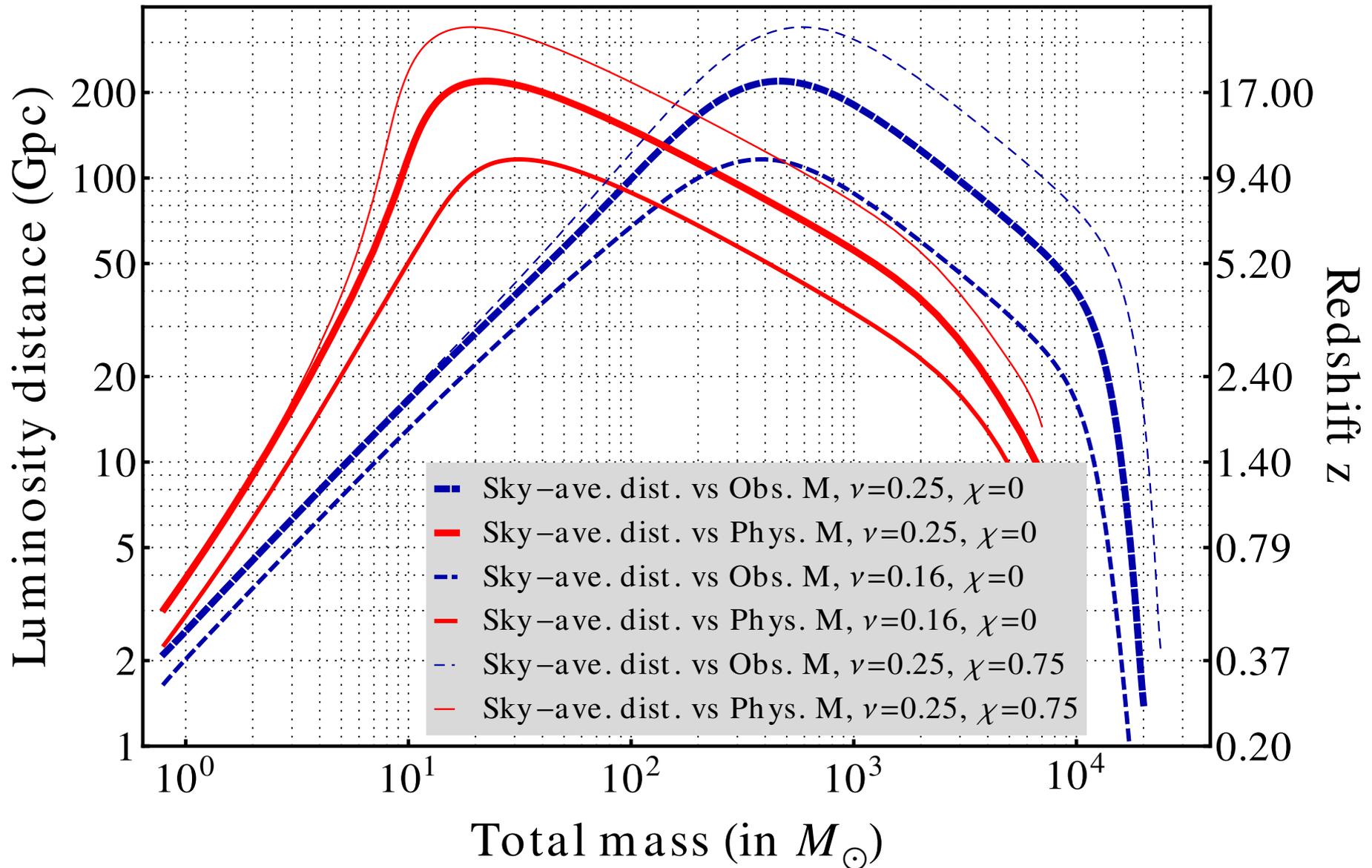
Caltech-Cornell Simulation

# Numerical Simulation of Merging Black Hole Binaries

Caltech-Cornell Simulation



# ET Distance Reach for Compact Binary Mergers



# Gravity's Standard Sirens

- To measure the luminosity distance to a source we need its **apparent** and **absolute** luminosities
- Gravitational wave observations of compact binary inspirals can measure both
  - **Apparent luminosity**: this is GW strain in our detector
  - **Absolute luminosity**: this is the rate at which GW frequency changes with time
- Therefore, binary black hole inspirals are **self-calibrating standard sirens**
- However, GW observations alone **cannot determine the red-shift** to a source
- Joint gravitational-wave and optical observations can facilitate a **new cosmological tool**

# Fundamental Physics

- Properties of gravitational waves
  - Testing GR beyond the quadrupole formula
    - Binary pulsars consistent with quadrupole formula; they don't measure properties of GW
  - How many polarizations are there?
    - In Einstein's theory only two polarizations; a scalar-tensor theory could have six
  - Do gravitational waves travel at the speed of light?
    - There are strong motivations from string theory to consider massive gravitons
    - Binary pulsars constrain the speed to few parts in a thousand
    - GW observations can constrain to 1 part in  $10^{18}$
- EoS of dark energy
  - Black hole binaries are standard candles/sirens
- EoS of supra-nuclear matter
  - Signature of EoS in GW emitted when neutron stars merge
- Black hole no-hair theorem and cosmic censorship
  - Are BH (candidates) of nature BH of general relativity?
- An independent constraint/measurement of neutrino mass
  - Delay in the arrival times of neutrinos and gravitational waves

# Do gravitational waves travel at the speed of light?

- Coincident observation of a supermassive black hole binary and the associated gravitational radiation can be used to constrain the speed of gravitational waves:
- If  $\Delta t$  is the time difference in the arrival times of GW and EM radiation and  $D$  is the distance to the source then the fractional difference in the speeds is

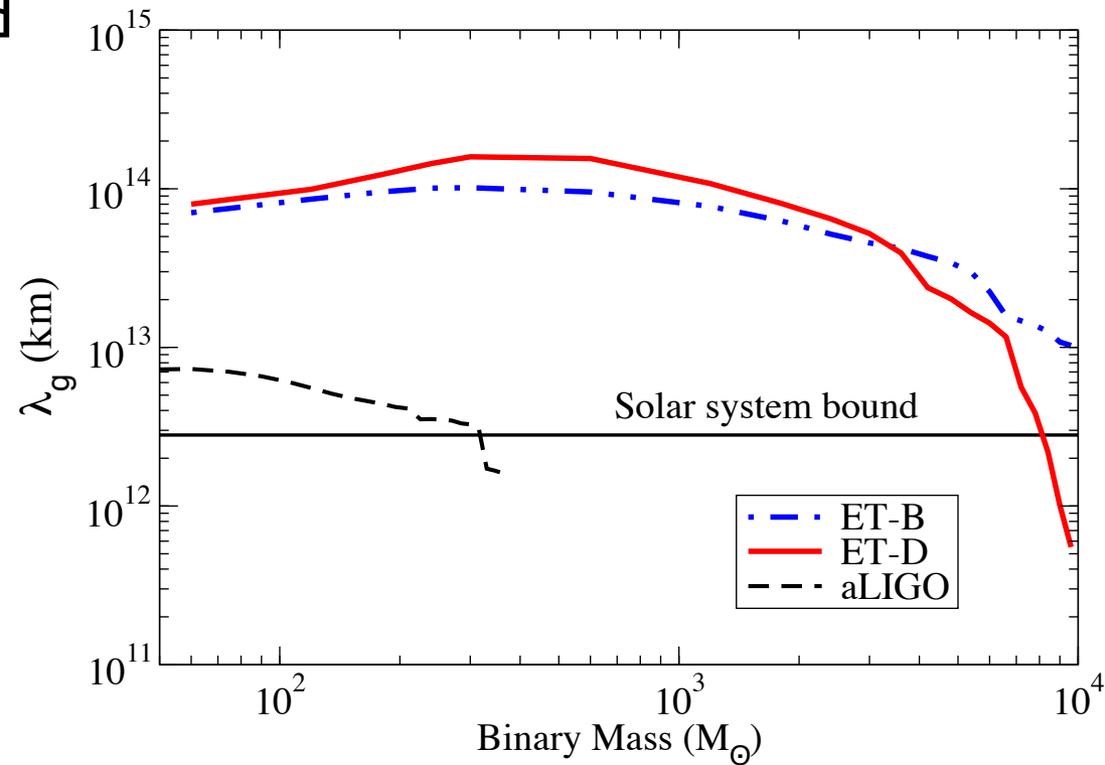
$$\frac{\Delta v}{c} = \frac{\Delta t}{D/c} \simeq 10^{-14} \left( \frac{\Delta t}{1\text{sec}} \right) \left( \frac{D}{1\text{Mpc}} \right)$$

- It is important to study what the EM signatures of massive BBH mergers are
- Can be used to set limits on the mass of the graviton slightly better than the current limits.

Will (1994, 98)

# Bound on graviton Compton wave length as a function of total mass

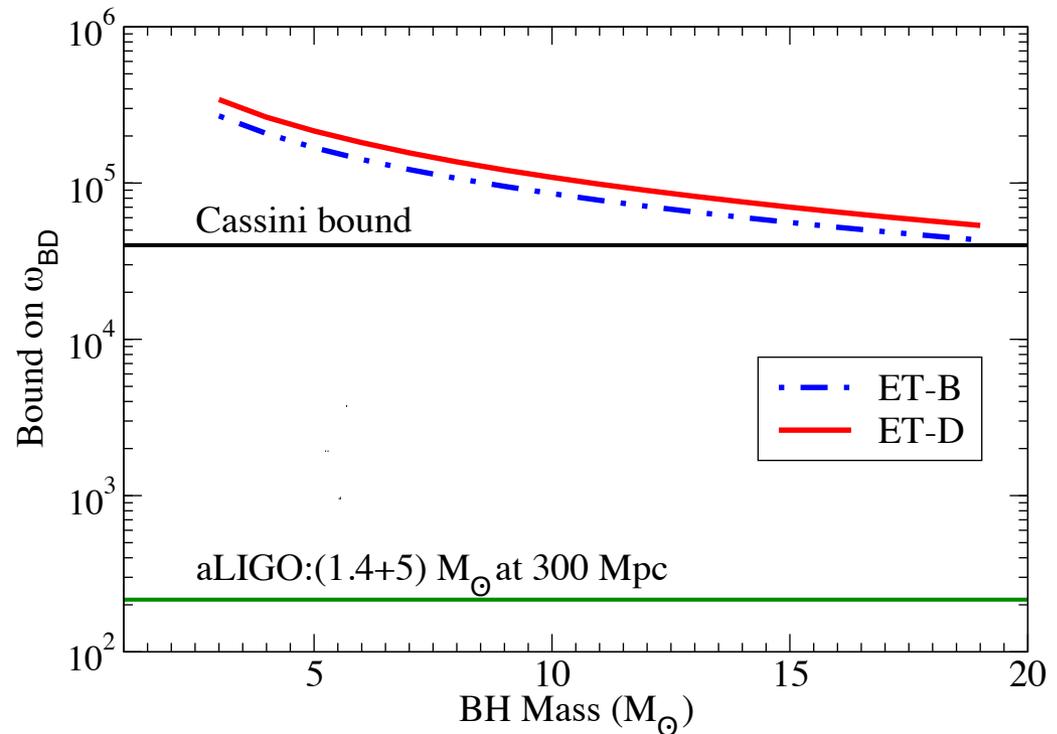
- The Compton wavelength of a particle is determined by its mass
- The larger the mass smaller will be its wavelength
- Limit on the Compton wavelength of graviton based on ET observations will be two orders-of-magnitude better than solar system limits



Arun and Will (2009)

# Testing Brans-Dicke Theory - An Alternative to Einstein's gravity

- Brans-Dicke theory has a parameter denoted  $\omega_{\text{BD}}$ . In Einstein's gravity this parameter takes the value infinity.
- ET can constrain this value by an order of magnitude more than current limits

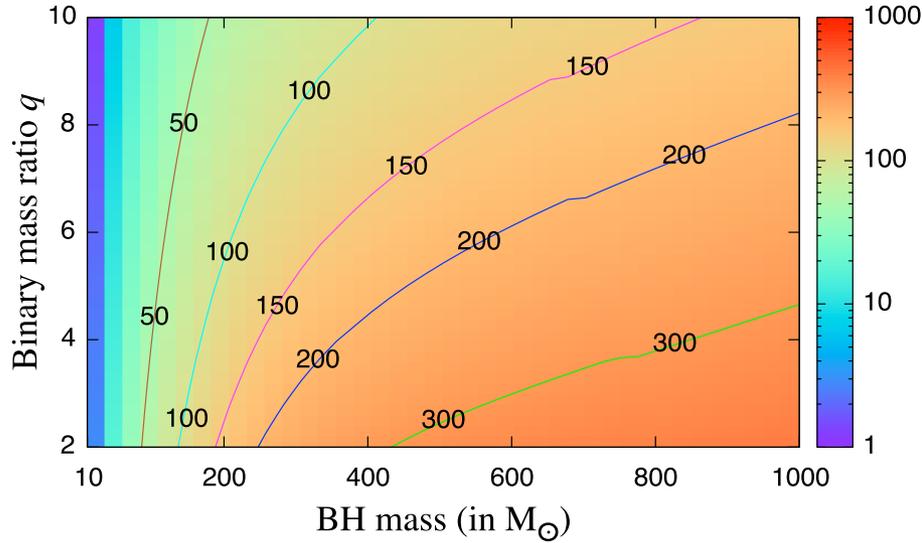


# Black Hole No-Hair Theorem

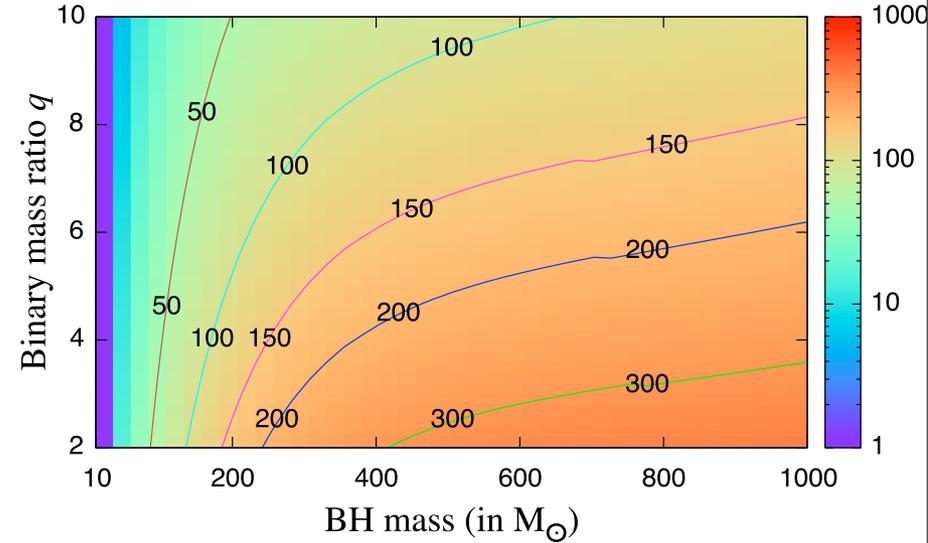
- Deformed black holes are unstable; they emit energy in their deformation as gravitational waves
  - Superposition of damped waves with many different frequencies and decay times
  - In Einstein's theory, frequencies and decay times all depend only on the mass  $M$  and spin  $j$  of the black hole
- Measuring two or modes would constrain Einstein's theory or provide a smoking gun evidence of black holes
  - If modes depend on other parameters (e.g., the structure of the central object), then test of the consistency between different mode frequencies and damping times would fail
- The amplitude of the modes carry additional information about what caused the deformity

# Visibility of QNM in ET: Formation of BHs at $z=1$

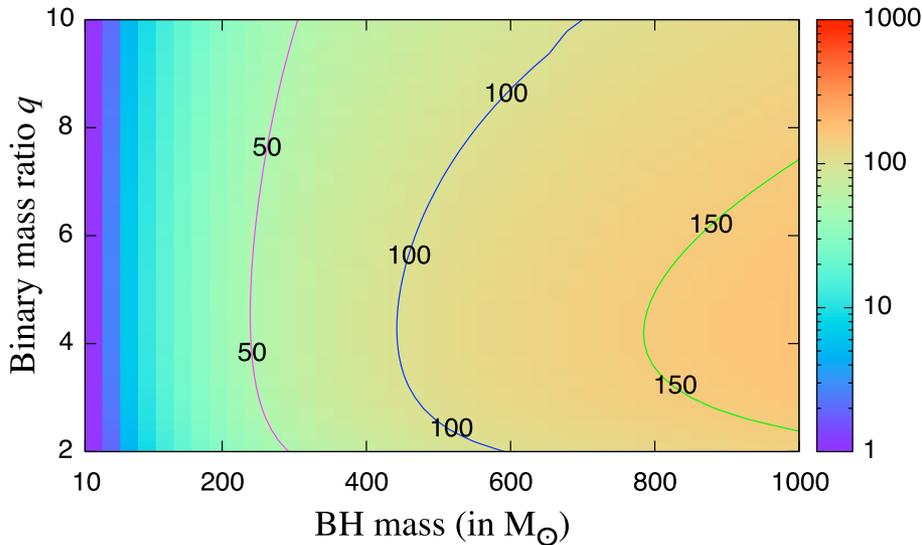
SNR in all modes



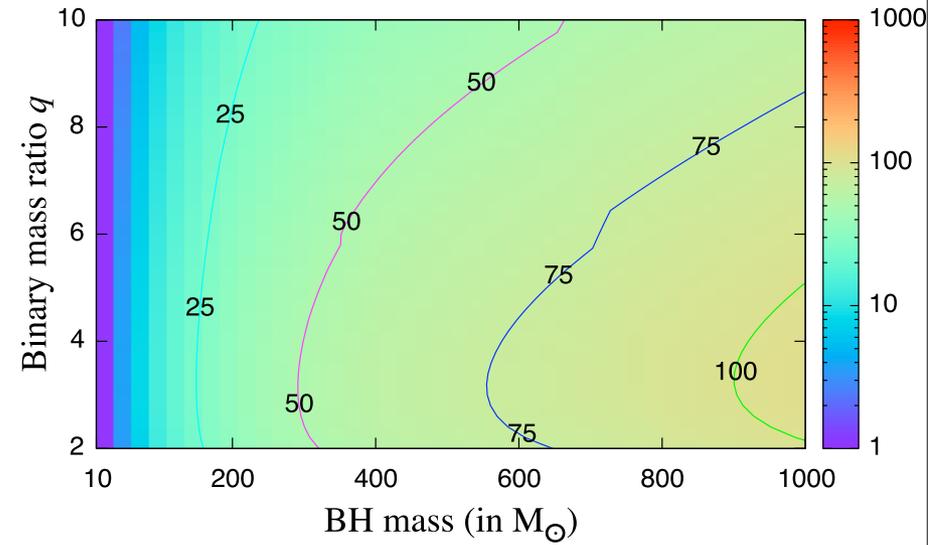
SNR in 22 mode



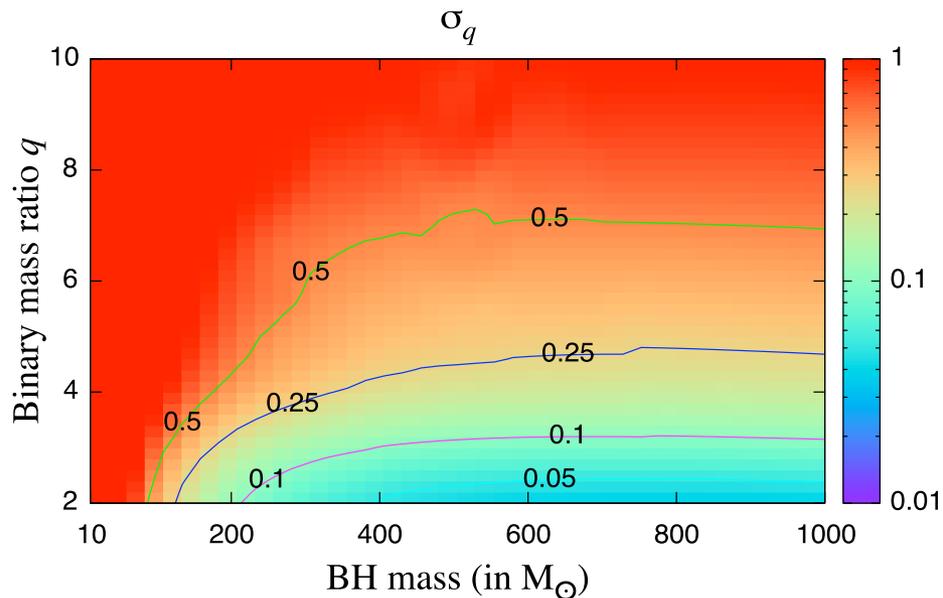
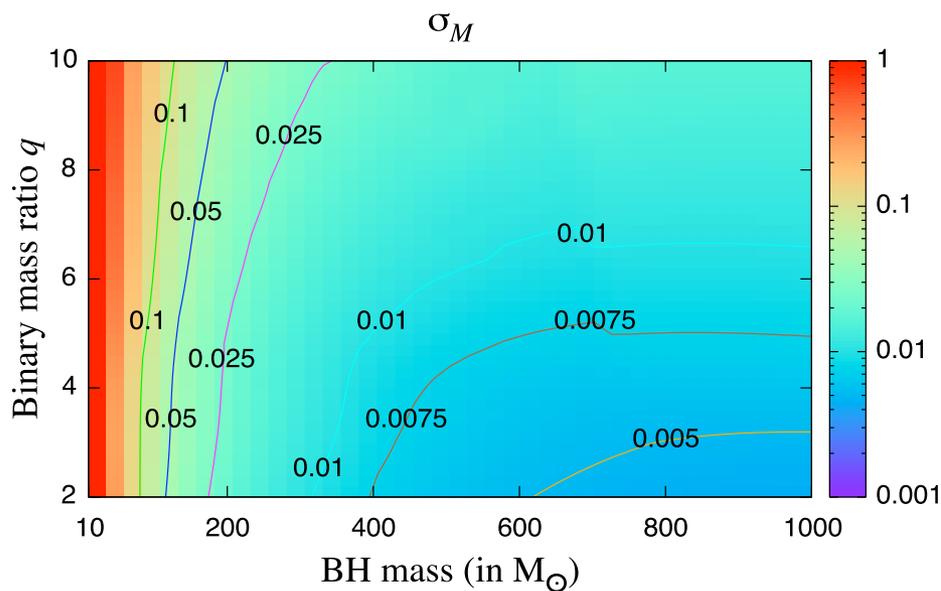
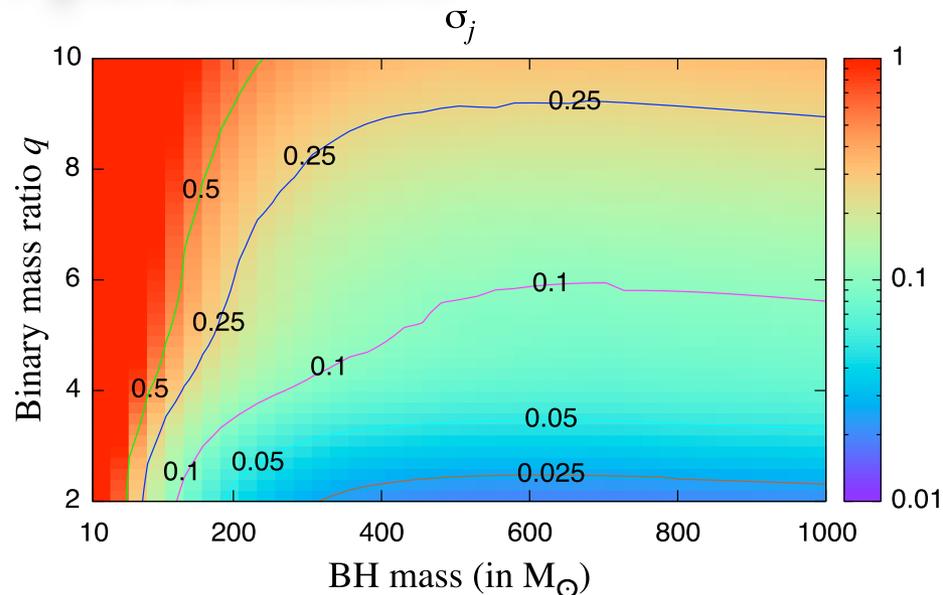
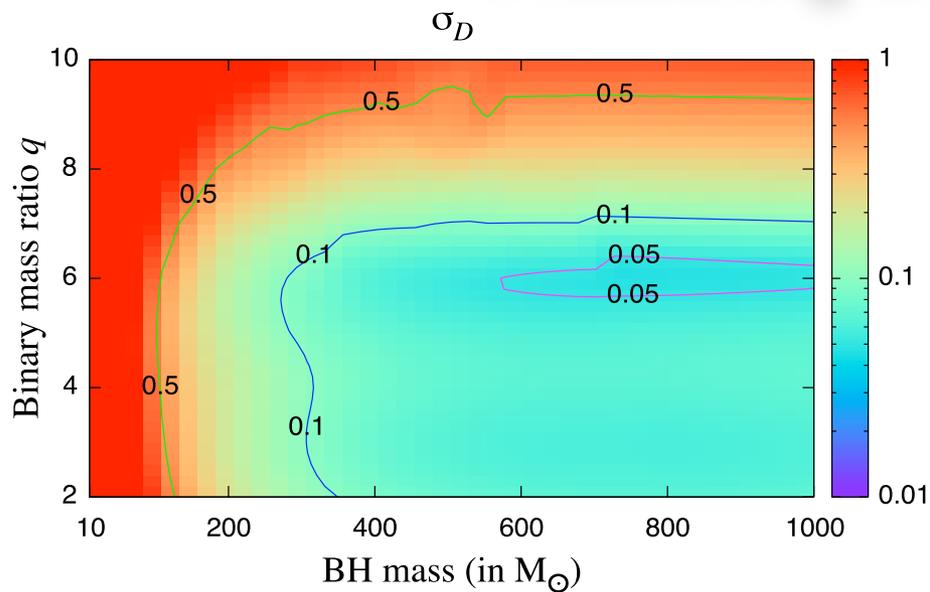
SNR in 33 mode



SNR in 21 mode



# Measuring BH parameters



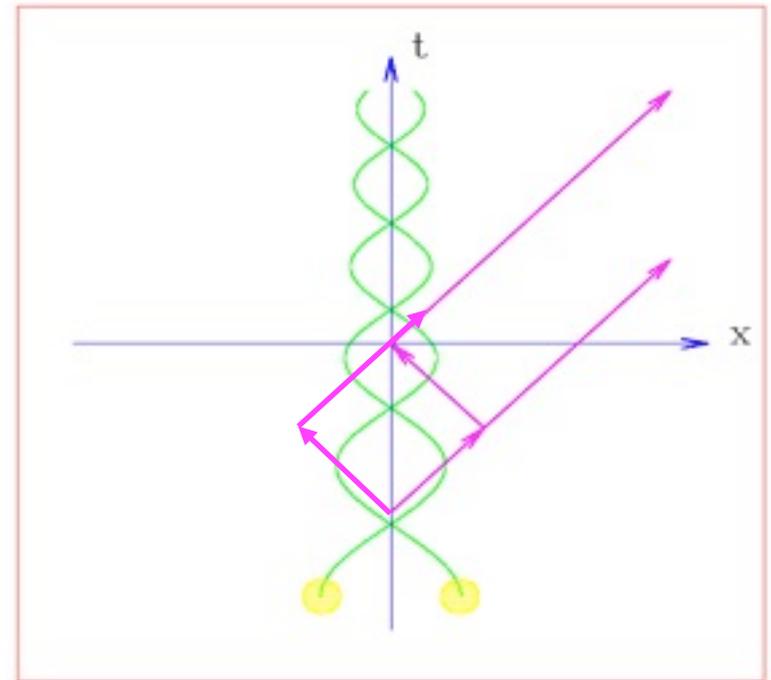
# BBH Signals as Testbeds for GR

- Gravity gets ultra-strong during a BBH merger compared to any observations in the solar system or in binary pulsars
  - In the solar system:  $\phi/c^2 \sim 10^{-6}$
  - In a radio binary pulsar it is still very small:  $\phi/c^2 \sim 10^{-4}$
  - Near a black hole  $\phi/c^2 \sim 1$
  - Merging binary black holes are the best systems for strong-field tests of GR
- Dissipative predictions of gravity are not even tested at the IPN level
  - In binary black holes even  $(v/c)^7$  PN terms will not be adequate for high-SNR ( $\sim 100$ ) events

# Testing GR by observing non-linear effects

- Binary inspiral waveform depends on many post-Newtonian coefficients
  - $\Psi_0, \Psi_2, \Psi_3, \dots$
  - They correspond to different physical effects, e.g. GW tails
- In the case of non-spinning binaries  $\Psi_0, \Psi_2, \Psi_3, \dots$  depend on just the two masses  $m_1$  and  $m_2$
- By assuming they are all independent one can check to see if GR is the correct theory

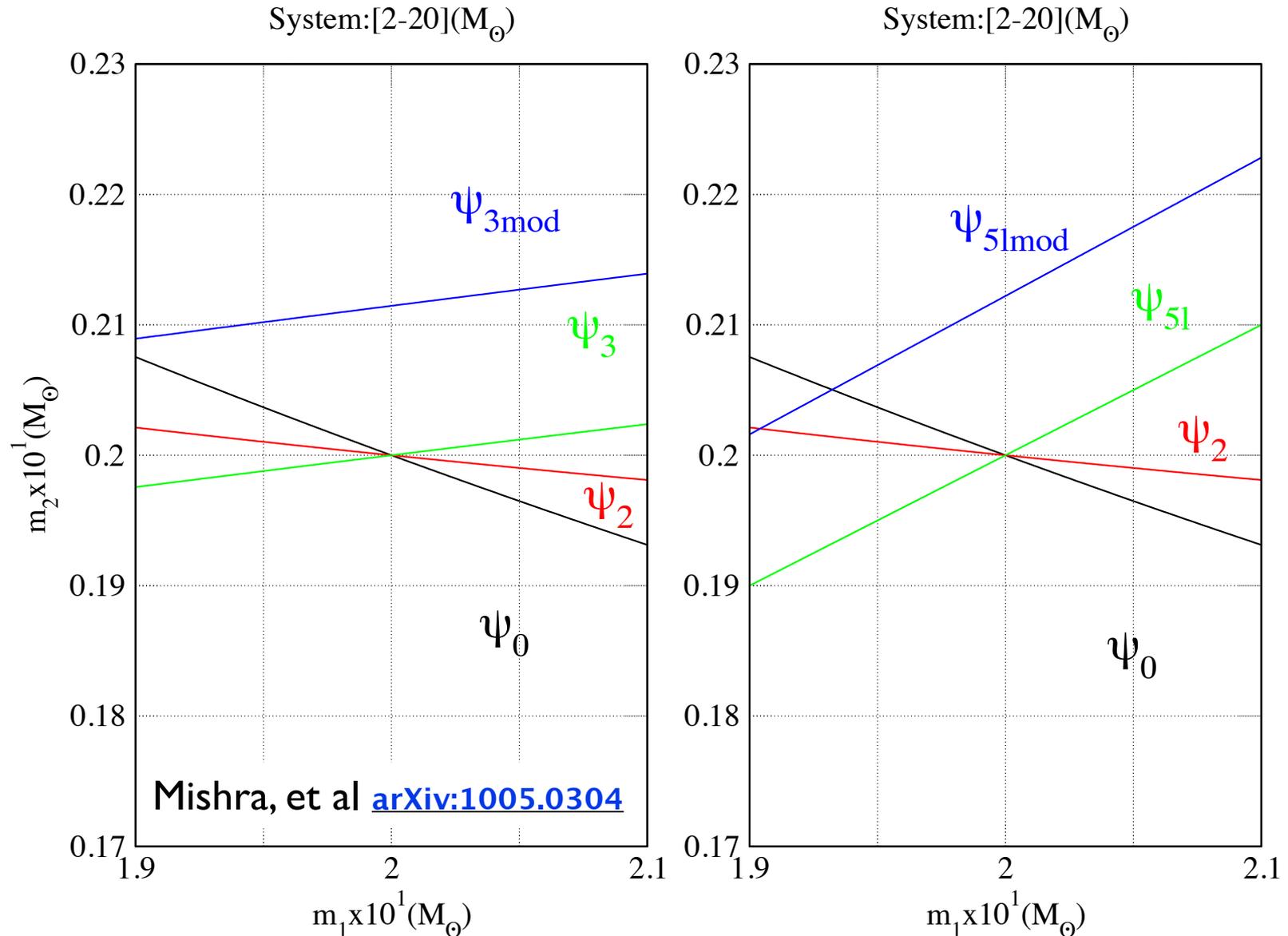
## Gravitational wave tails



Blanchet and Schaefer (1994)

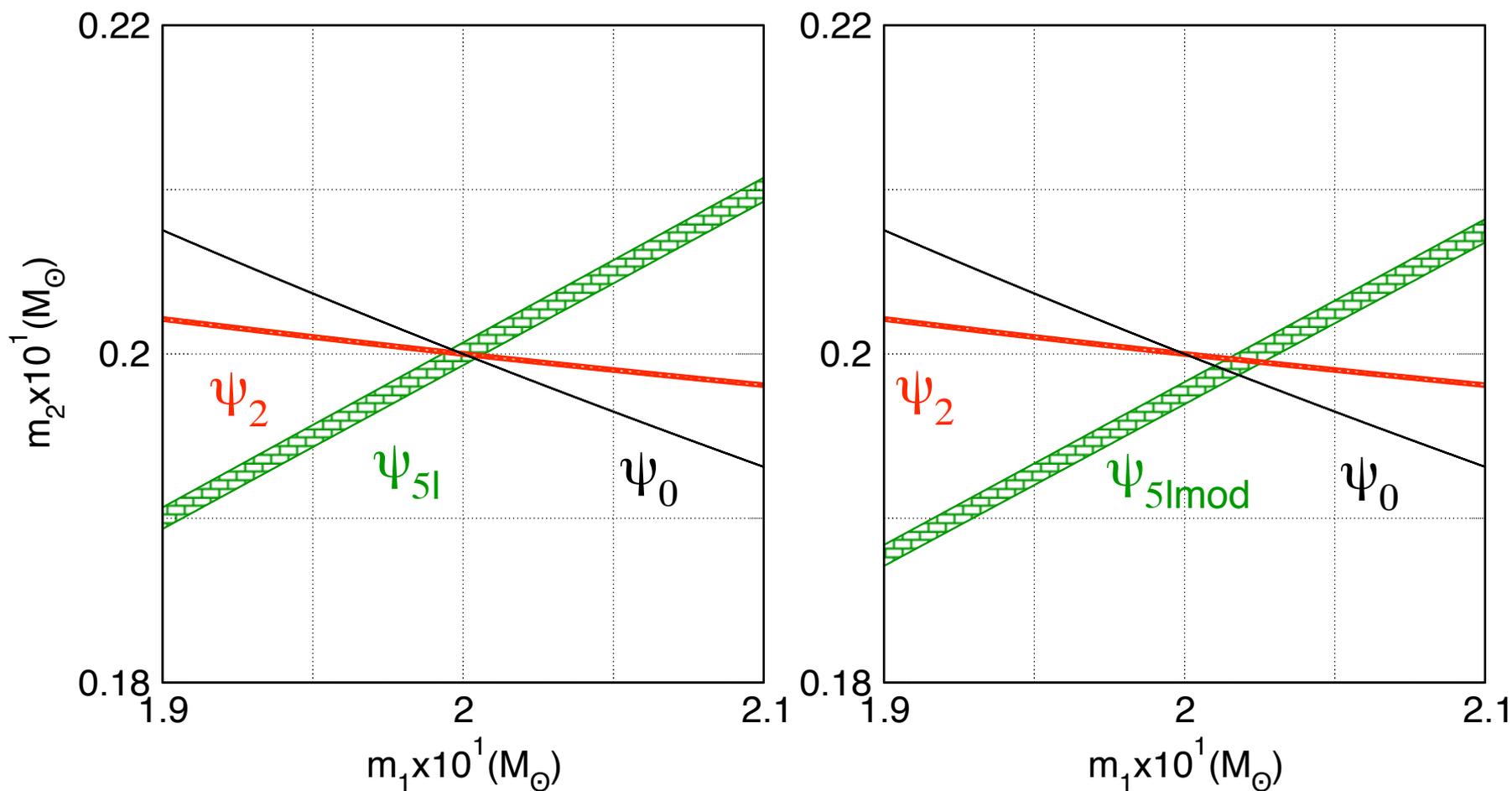
# What will we see if GR is not the correct theory?

Effect of changing the coefficients  $\psi_3$  and  $\psi_{51}$  by 5% on the test.



# How well can ET measure non-linear effects?

Model=RWF;  $q_m=0.1$ ;  $D_L=300\text{Mpc}$ ; ET-B;  $F_{\text{low}}=1\text{Hz}$ ;



Mishra, et al (2010)

# Cosmology

## ••• Cosmography

- Build the cosmic distance ladder, strengthen existing calibrations at high  $z$
- Measure the Hubble parameter, dark matter and dark energy densities, dark energy EoS  $w$ , variation of  $w$  with  $z$

## ••• Black hole seeds

- Black hole seeds could be intermediate mass black holes
- Might explore hierarchical growth of central engines of black holes

## ••• Dipole anisotropy in the Hubble parameter

- The Hubble parameter will be “slightly” different in different directions due to the local flow of our galaxy

## ••• Anisotropic cosmologies

- In an anisotropic Universe the distribution of  $H$  on the sky should show residual quadrupole and higher-order anisotropies

## ••• Primordial gravitational waves

- Quantum fluctuations in the early Universe could produce a stochastic b/g

## ••• Production of GW during early Universe phase transitions

- Phase transitions, pre-heating, re-heating, etc., could produce detectable stochastic GW

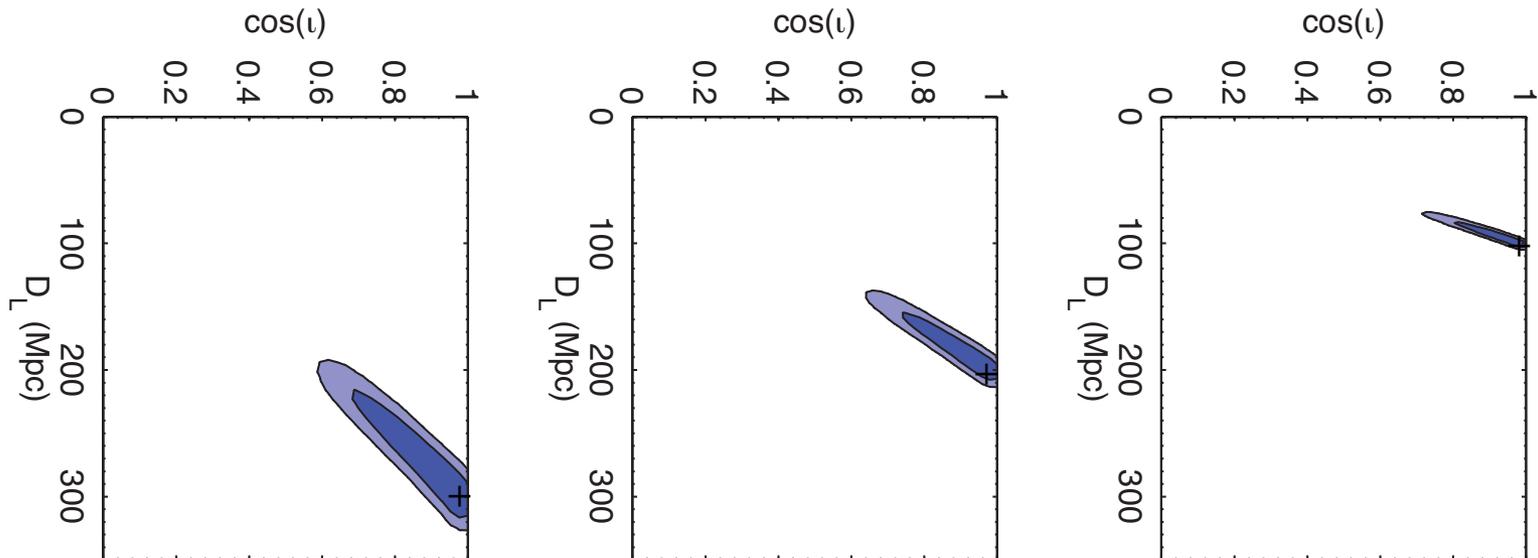
# Hubble Constant from Advanced Detectors

EXPLORING SHORT GAMMA-RAY BURSTS AS GRAVITATIONAL-WAVE STANDARD SIRENS

SAMAYA NISSANKE<sup>1,2</sup>, SCOTT A. HUGHES<sup>2</sup>, DANIEL E. HOLZ<sup>3</sup>, NEAL DALAL<sup>1</sup>, JONATHAN L. SIEVERS<sup>1</sup>

*Draft version April 7, 2009*

is further augmented by a factor of 1.12. To this end, we find that *one* year of observation should be enough to measure  $H_0$  to an accuracy of  $\sim 1\%$  if SHBs are dominated by beamed NS-BH binaries using the “full” network of LIGO, Virgo, AIGO, and LCGT—admittedly,

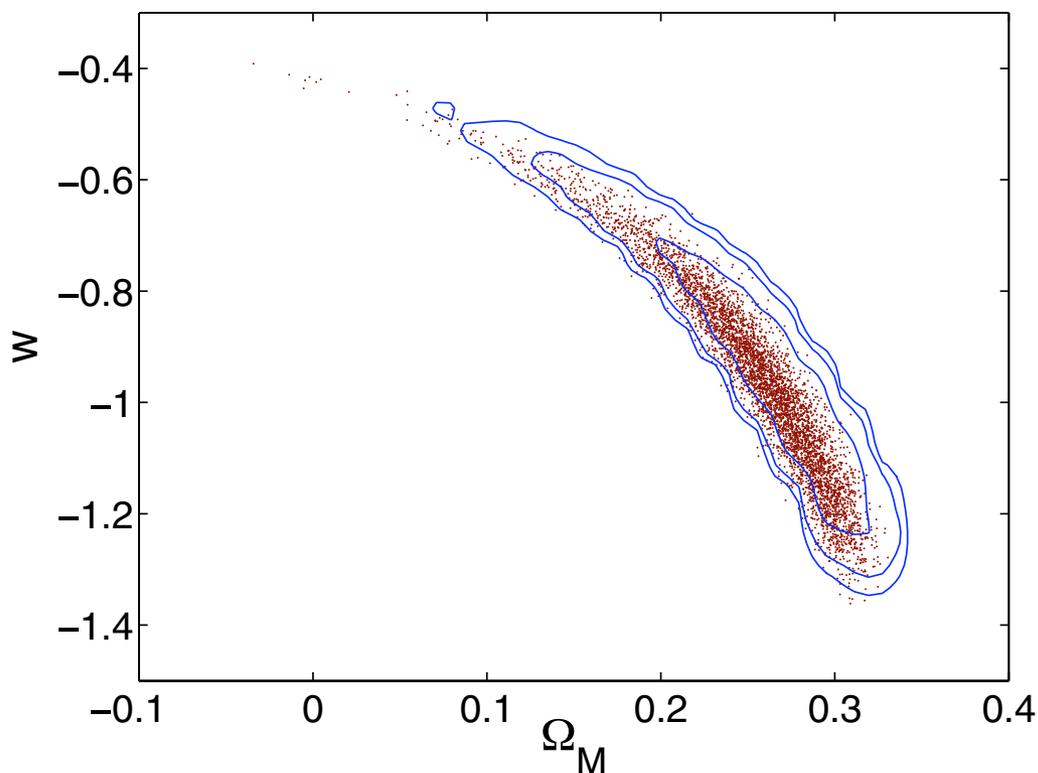


# ET: Measuring Dark Energy and Dark Matter

- ET will observe 100's of binary neutron stars and GRB associations each year
- GRBs could give the host location and red-shift, GW observation provides  $D_L$

Class. Quantum Grav. **27** (2010) 215006

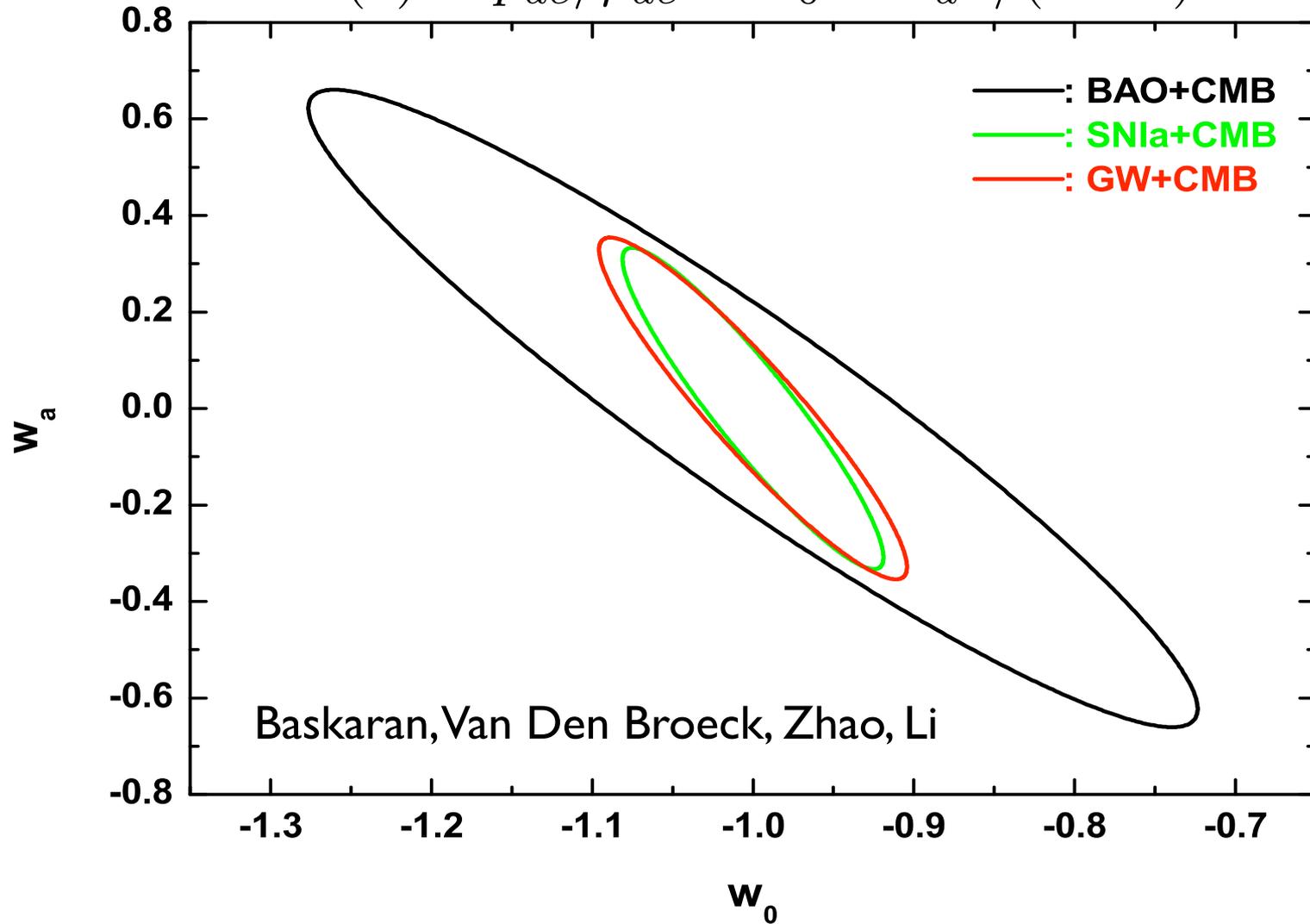
B S Sathyaprakash *et al*



**Figure 3.** Scatter plot of the retrieved values for  $(\Omega_\Lambda, w)$ , with 1- $\sigma$ , 2- $\sigma$  and 3- $\sigma$  contours, in the case where weak lensing is not corrected.

# Measuring $w$ and its variation with $z$

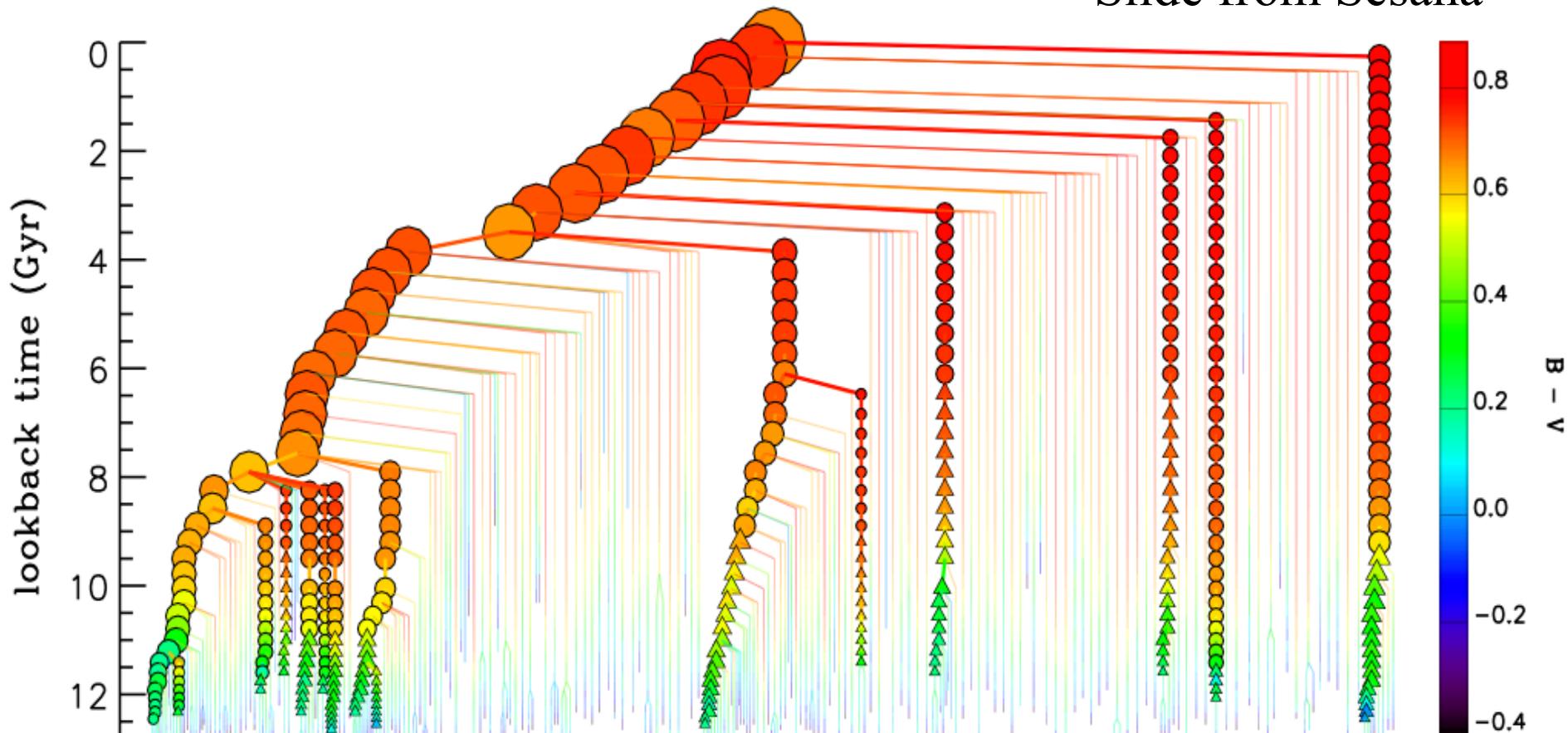
$$w(z) \equiv p_{de}/\rho_{de} = w_0 + w_a z/(1+z)$$



Baskaran, Van Den Broeck, Zhao, Li

# Hierarchical Growth of Black Holes in Galactic Nuclei

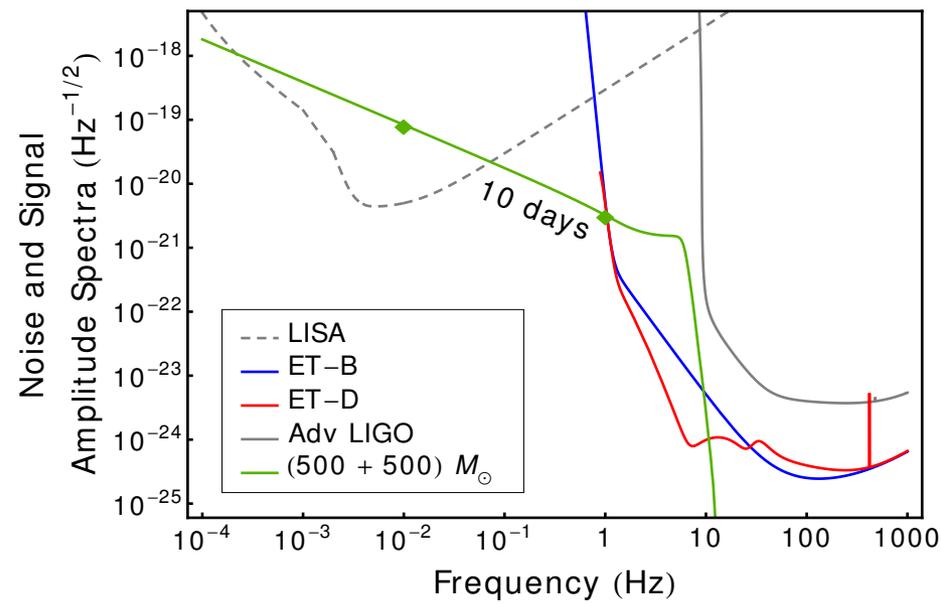
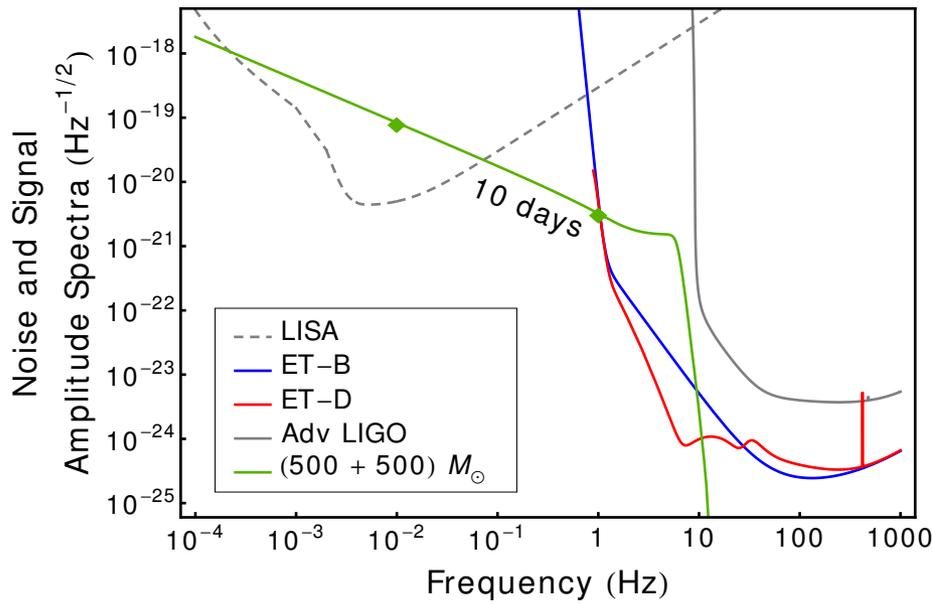
Slide from Sesana



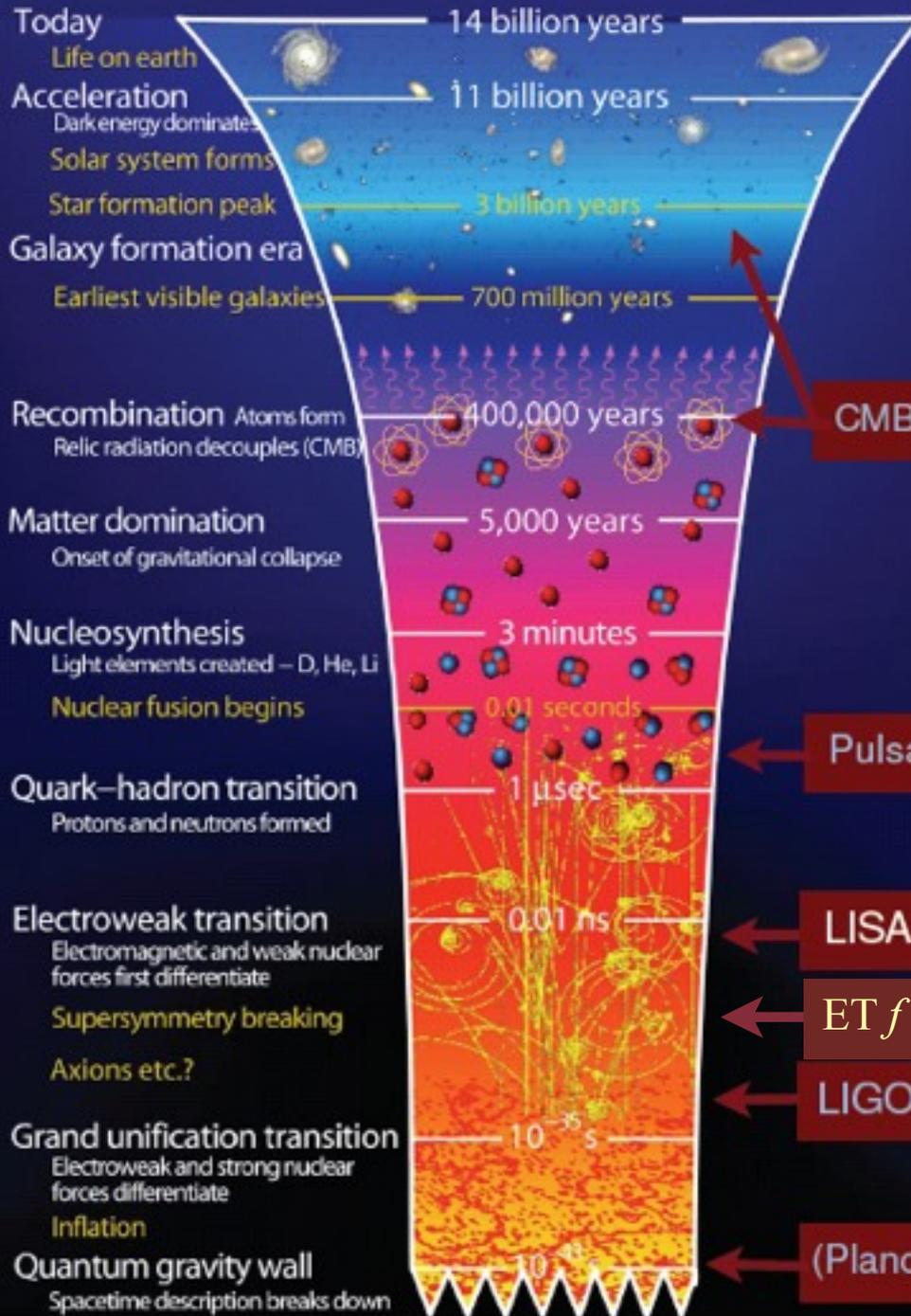
- Initially small black holes may grow by hierarchical merger
- ET could observe seed black holes if they are of order 1000 solar mass

# Observing Intermediate-mass Black Hole Binaries

- Ultra-luminous X-ray sources might be hosting black holes of mass one thousand solar masses
- 100 solar mass black holes could be seeds of galaxy formation
- ET could observe black hole populations at different red-shifts and resolve questions about black hole demographics



# A brief history of the Universe



CMB  $f < 3 \times 10^{-17} h\text{Hz}$  probes  $300,000\text{yrs} < t_e < 14\text{Gyrs}$

Pulsars  $f \sim 10^{-8}\text{Hz}$  probe  $t_e \sim 10^{-4}\text{s}$  ( $T \sim 50\text{MeV}$ )

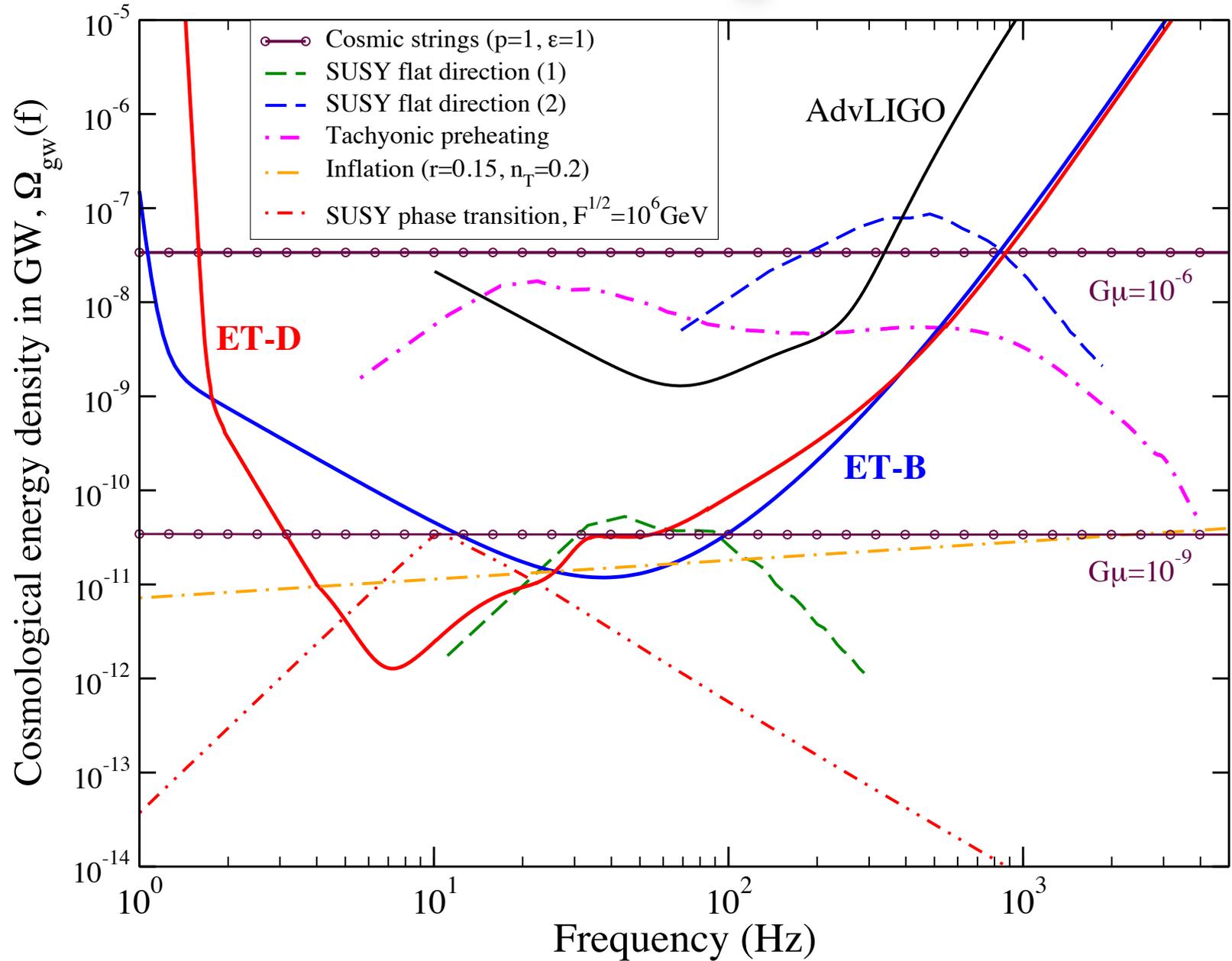
LISA  $f \sim 10^{-3}\text{Hz}$  probes  $t_e \sim 10^{-14}\text{s}$  ( $T \sim 10\text{TeV}$ )

ET  $f \sim 10\text{Hz}$  probes  $t_e \sim 10^{-20}\text{s}$  ( $T \sim 10^6\text{GeV}$ )

LIGO  $f \sim 100\text{Hz}$  probes  $t_e \sim 10^{-24}\text{s}$  ( $T \sim 10^8\text{GeV}$ )

(Planck scale  $f \sim 10^{11}\text{Hz}$  has  $t_e \sim 10^{-43}\text{s}$  ( $T \sim 10^{19}\text{GeV}$ ))

# Primordial Backgrounds

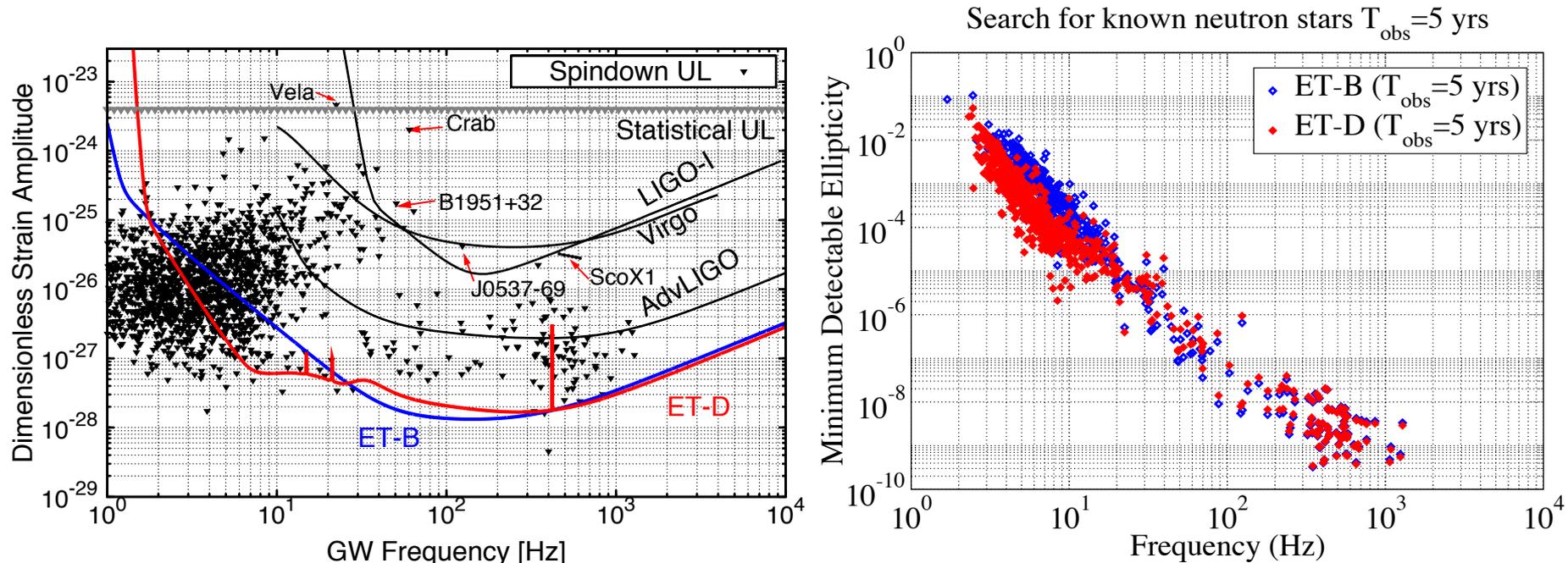


# Astrophysics

- Unveiling progenitors of short-hard GRBs
  - Understand the demographics and different classes of short-hard GRBs
- Understanding Supernovae
  - Astrophysics of gravitational collapse and accompanying supernova?
- Evolutionary paths of compact binaries
  - Evolution of compact binaries involves complex astrophysics
    - Initial mass function, stellar winds, kicks from supernova, common envelope phase
- Finding why pulsars glitch and magnetars flare
  - What causes sudden excursions in pulsar spin frequencies and what is behind ultra high-energy transients of EM radiation in magnetars
    - Could reveal the composition and structure of neutron star cores
- Ellipticity of neutron stars as small as 1 part in a billion ( $10\mu\text{m}$ )
  - Mountains of what size can be supported on neutron stars?
- NS spin frequencies in LMXBs
  - Why are spin frequencies of neutron stars in low-mass X-ray binaries bounded?
- Onset/evolution of relativistic instabilities
  - CFS instability and r-modes

# Mountains on Neutron Stars

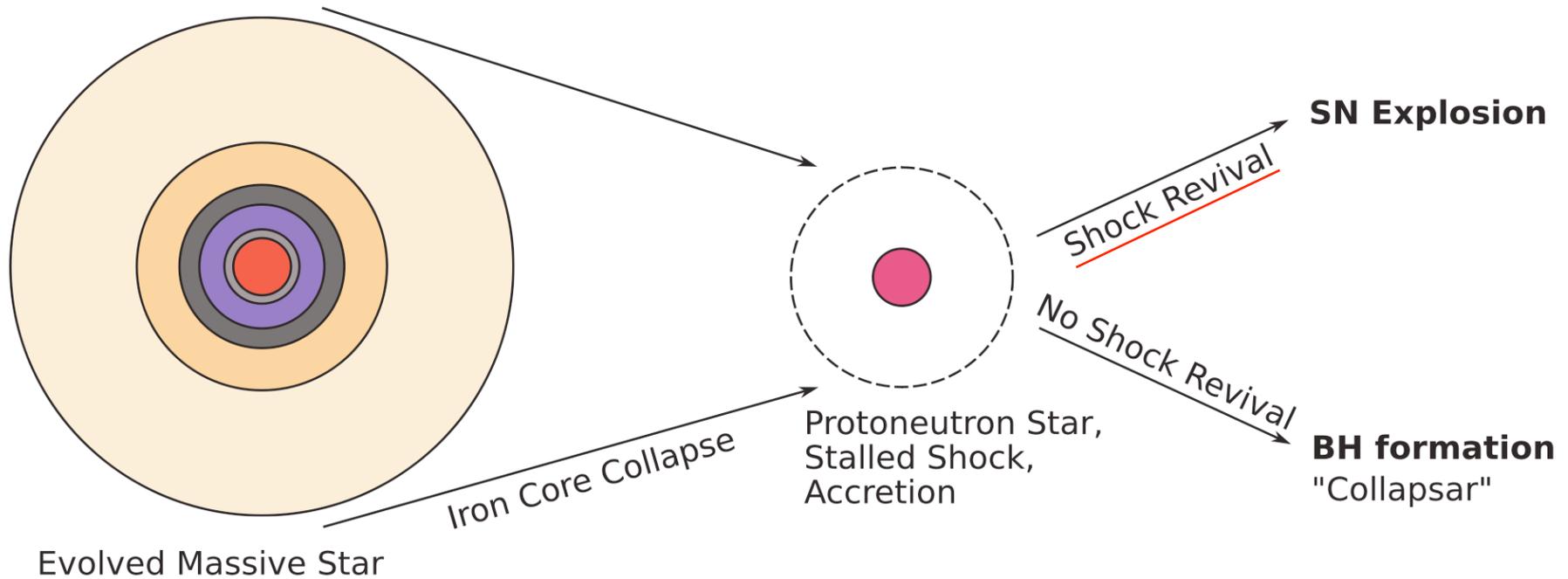
- ET will check if neutron stars (10 km in radius) have mountains that are smaller than 10 micro meters
- This could constrain models about their crustal strengths



# Supernovae

- Standard candles of astronomy
  - Our knowledge of the expansion rate of the Universe at redshift of  $z=1$  comes from SNe
- Produce dust and affect evolution of galaxies
  - Heavy elements are only produced in SNe
- They are precursors to formation of neutron stars and black holes
  - The most compact objects in the Universe
- SNe cores are laboratories of complex physical phenomena
  - Most branches of physics and astrophysics needed in modelling
    - General relativity, nuclear physics, relativistic magnetohydrodynamics, turbulence, neutrino viscosity and transport, ...
- Unsolved problem: what is the mechanism of shock revival?

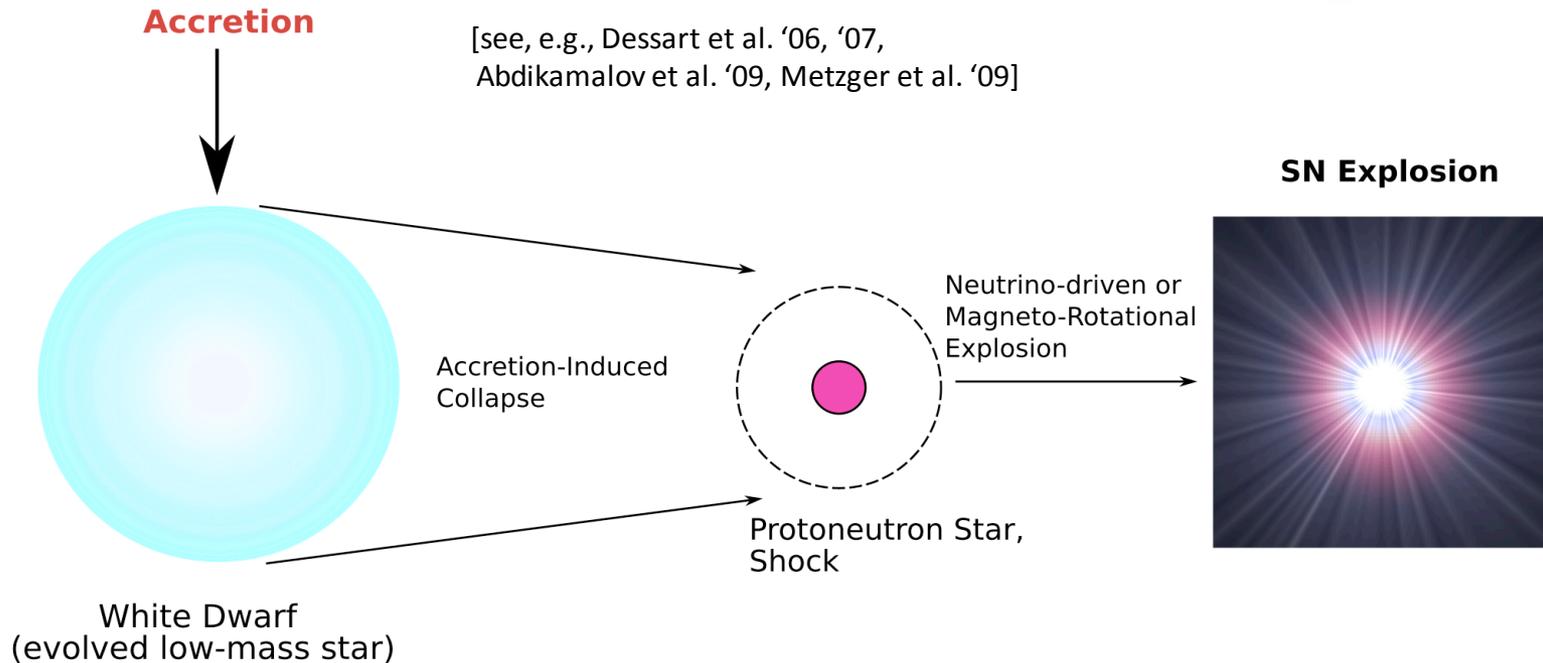
# Core Collapse SNe



- Energy reservoir
  - few  $\times 10^{53}$  erg
- Explosion energy
  - $10^{51}$  erg

- Time frame for explosion
  - 300 - 1500 ms after bounce
- Formation of black hole
  - At baryonic mass  $> 1.8-2.5 M$

# Accretion Induced Collapse

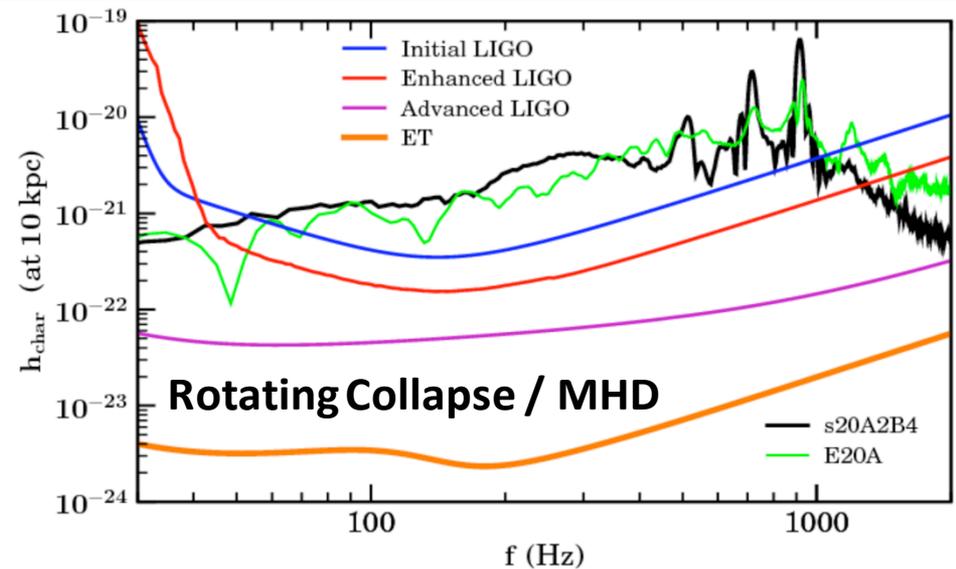
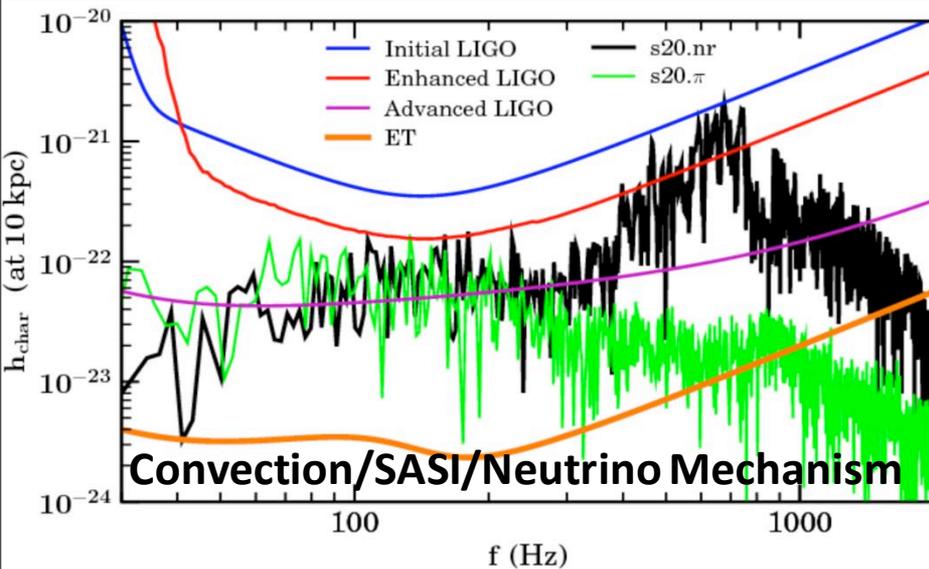
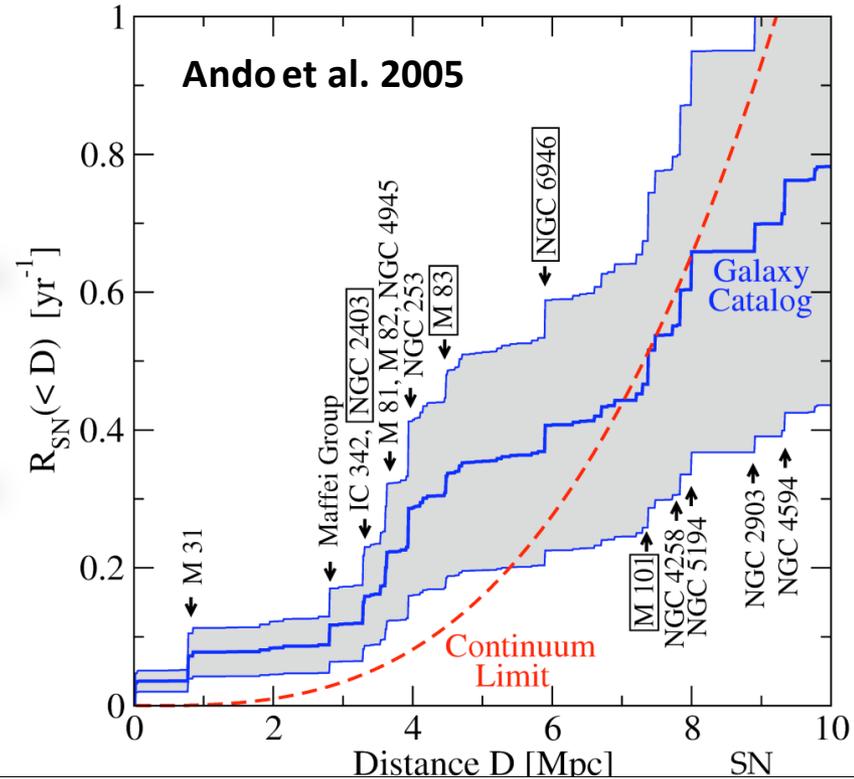


- Collapse of accreting, probably rotating White Dwarfs
- Neutrino-driven or magneto-rotational explosion
- Explosion probably weak, sub-luminous

- Might not be seen in optical
- Potential birth site of magnetars - highly ( $10^{15}$ -  $10^{16}$  G) magnetized neutron stars

# SNe Rate in ET

- ET sensitive to SNe up to 5 Mpc
- Could observe one SN once in few years
- Coincident observation with neutrino detectors
- Might be allow measurement of neutrino mass
- Plots show the spectra of SNe at 10 Kpc for two different models



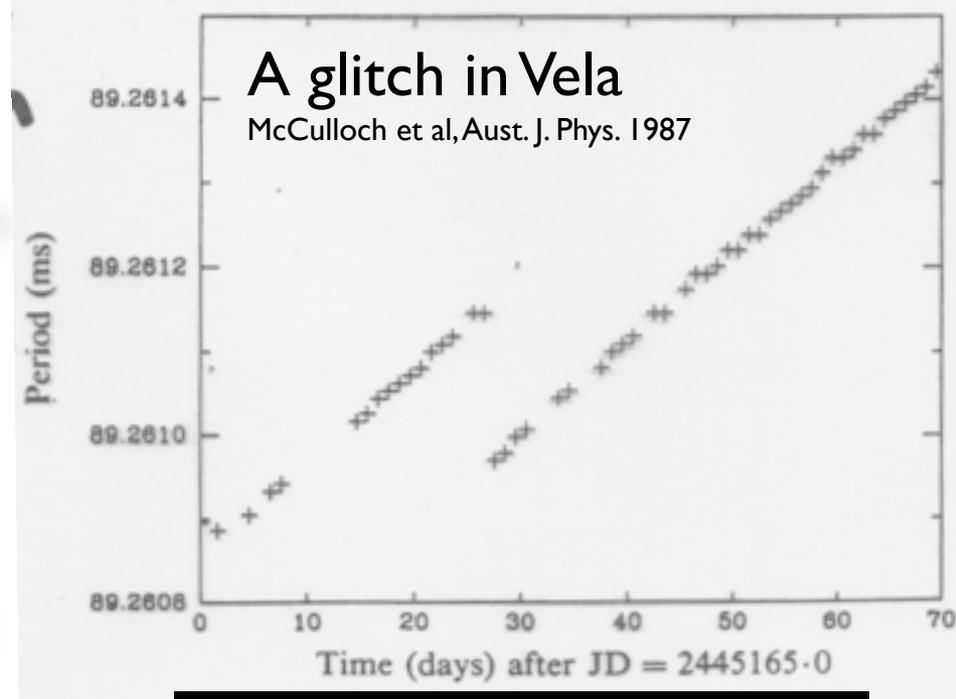
# Pulsar Glitches

- Pulsars have fairly stable rotation rates:
  - However, observe the secular increase in pulse period
- Glitches are sudden dips in the rotation period
  - Vela shows glitches once every few years
- Could be the result of transfer of angular momentum from core to crust
  - At some critical lag rotation rate of superfluid core couples to the crust, imparting energy to the crust

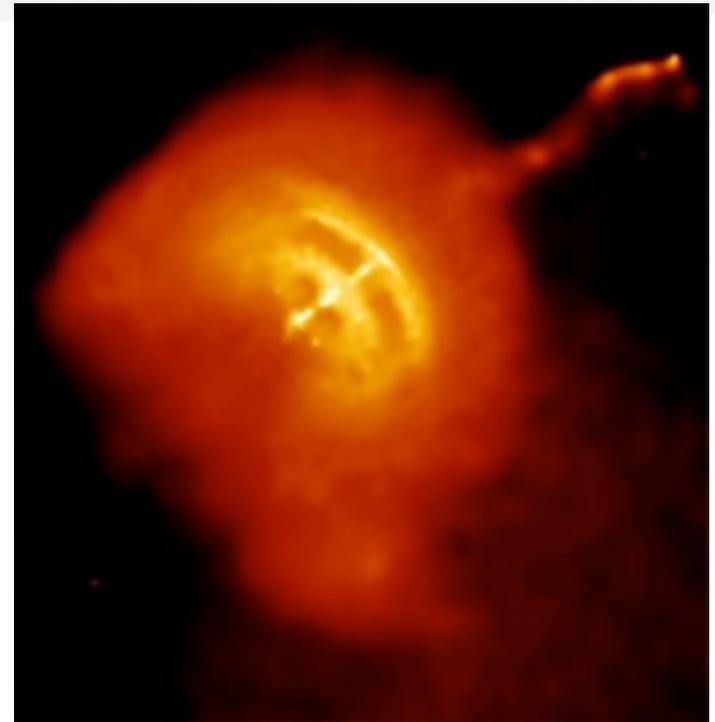
$$\Delta J \sim I_* \Delta \Omega \quad \Delta E = \Delta J \Omega_{\text{lag}}$$

$$\Delta \Omega / \Omega \sim 10^{-6}$$

$$\Delta E \sim 10^{-13} - 10^{-11} M_{\odot} c^2$$

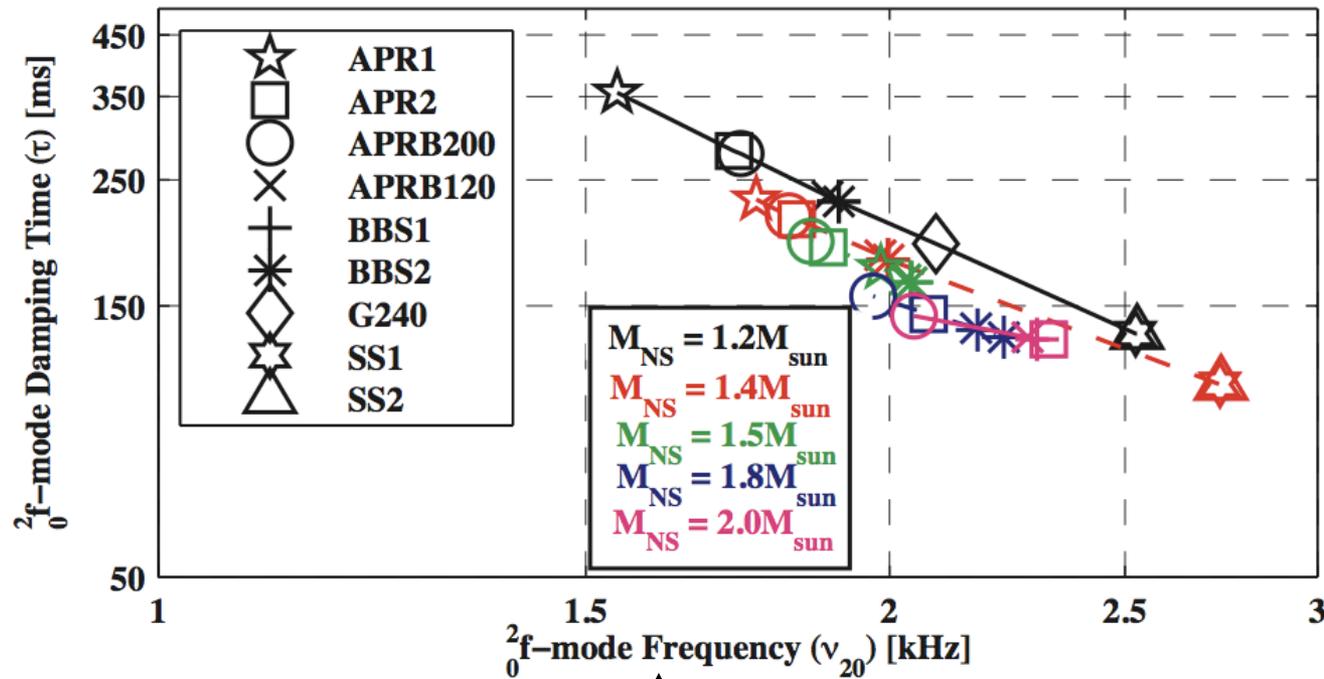
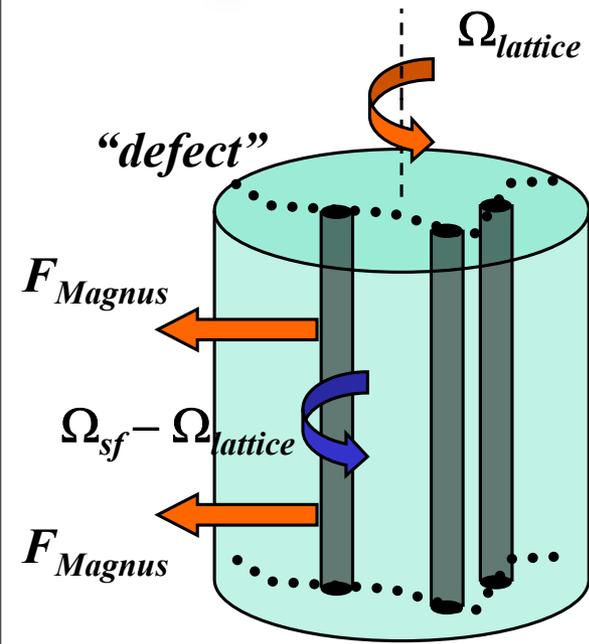


A composite Vela image



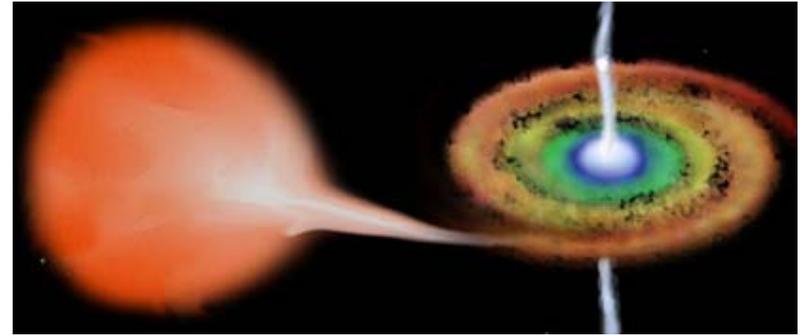
# NS Normal Mode Oscillations

- Sudden jolt due to a glitch, and superfluid vortex unpinning, could cause oscillations of the core, emitting gravitational waves
- These normal mode oscillations have characteristic frequencies and damping times that depend on the equation-of-state
- Detecting and measuring normal modes could reveal the equation-of-state of neutron stars and their internal structure



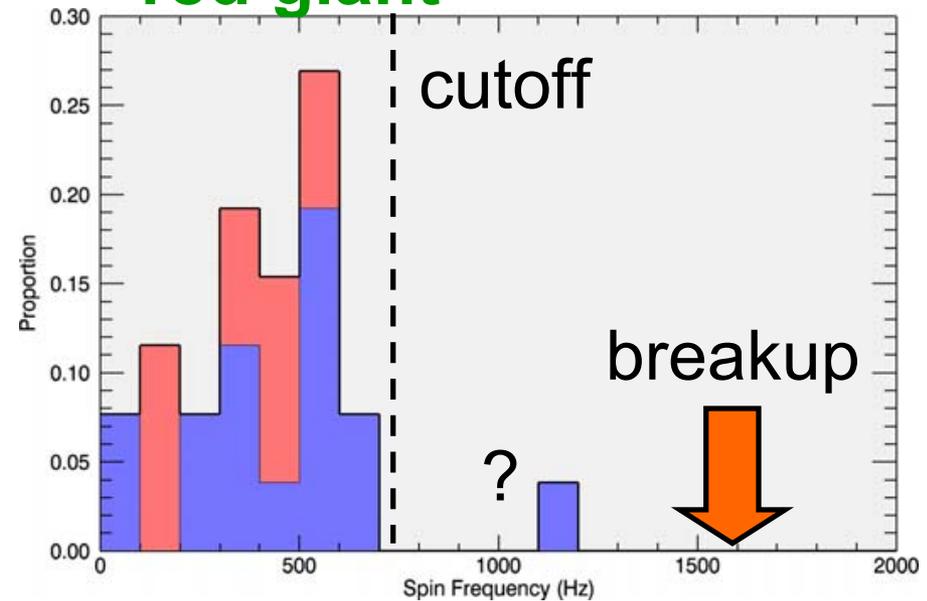
# Accreting Neutron Stars

- Spin frequencies of accreting NS seems to be stalled below 700 Hz
  - Well below the break-up speed
- What could be the reason for this stall?
  - Balance of accretion torque with GW back reaction torque
- Could be explained if ellipticity is  $\sim 10^{-8}$ 
  - Could be induced by mountains or relativistic instabilities, e.g. r-modes



$< 1M_{\text{Sun}}$   
red giant

NS



pulses & burst oscillations

# Summary of Science with ET

## •• Fundamental Physics

- Is the nature of gravitational radiation as predicted by Einstein?
- Is Einstein theory the correct theory of gravity?
- Are black holes in nature black holes of GR?
- Are there naked singularities?

## •• Astrophysics

- What is the nature of gravitational collapse?
- What is the origin of gamma ray bursts?
- What is the structure of neutron stars and other compact objects?

## •• Cosmology

- How did massive black holes at galactic nuclei form and evolve?
- What is dark energy?
- What phase transitions took place in the early Universe?
- What were the physical conditions at the big bang?