

# COMPARISON OF PARAMETER ESTIMATION BETWEEN ET-B AND ET-C SENSITIVITIES

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# Topics

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Outline

## Cosmology

- Infer characteristics of the universe
- Measured parameters  
 $(\Omega_M, \Omega_\Lambda, \Omega_k, w_0, w_a)$

## Testing General Relativity

- Test GR through its phase evolution
- Measured parameters  
 $(\phi_0, \phi_2, \phi_3, \dots)$

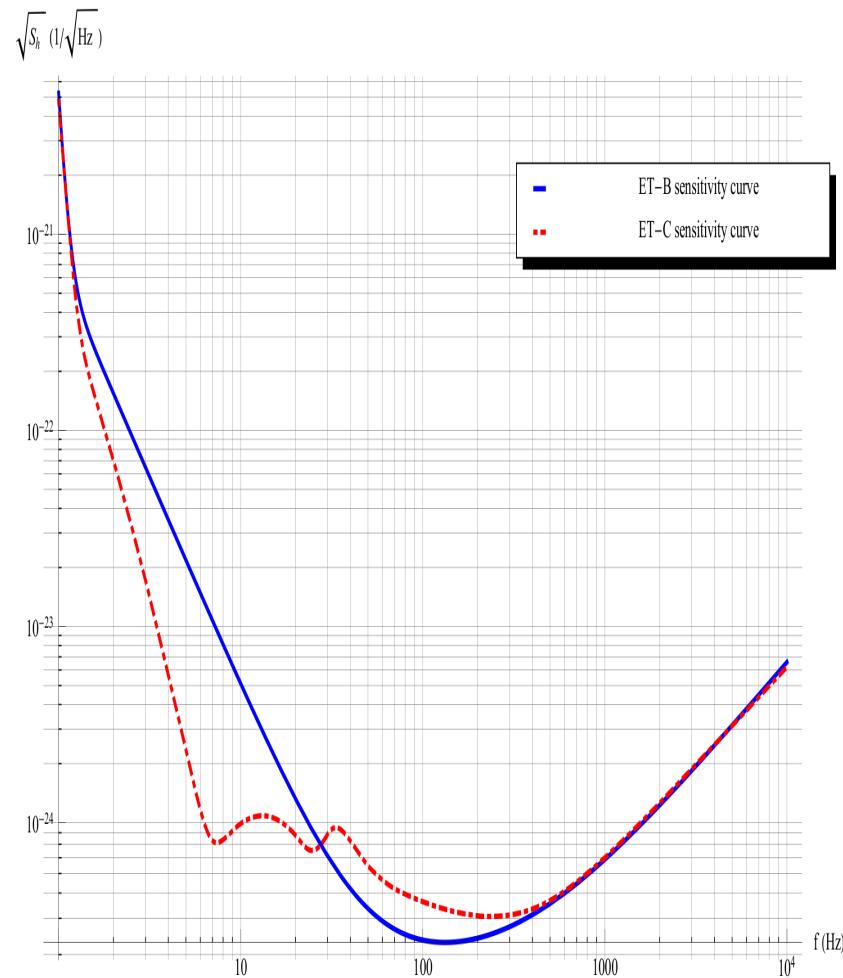


Compare parameter estimation for different Einstein Telescope design studies

# Design Sensitivities

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Outline



- **ET-B**
  - Single 3rd generation broadband detector
- **ET-C: Xylophone**
  - 2 band interferometer
  - high-power, high-frequency
  - cryogenic low-power, low-frequency

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# Cosmography

Infer characteristics of the universe by observing  
coalescing binary neutron stars

# Cosmology

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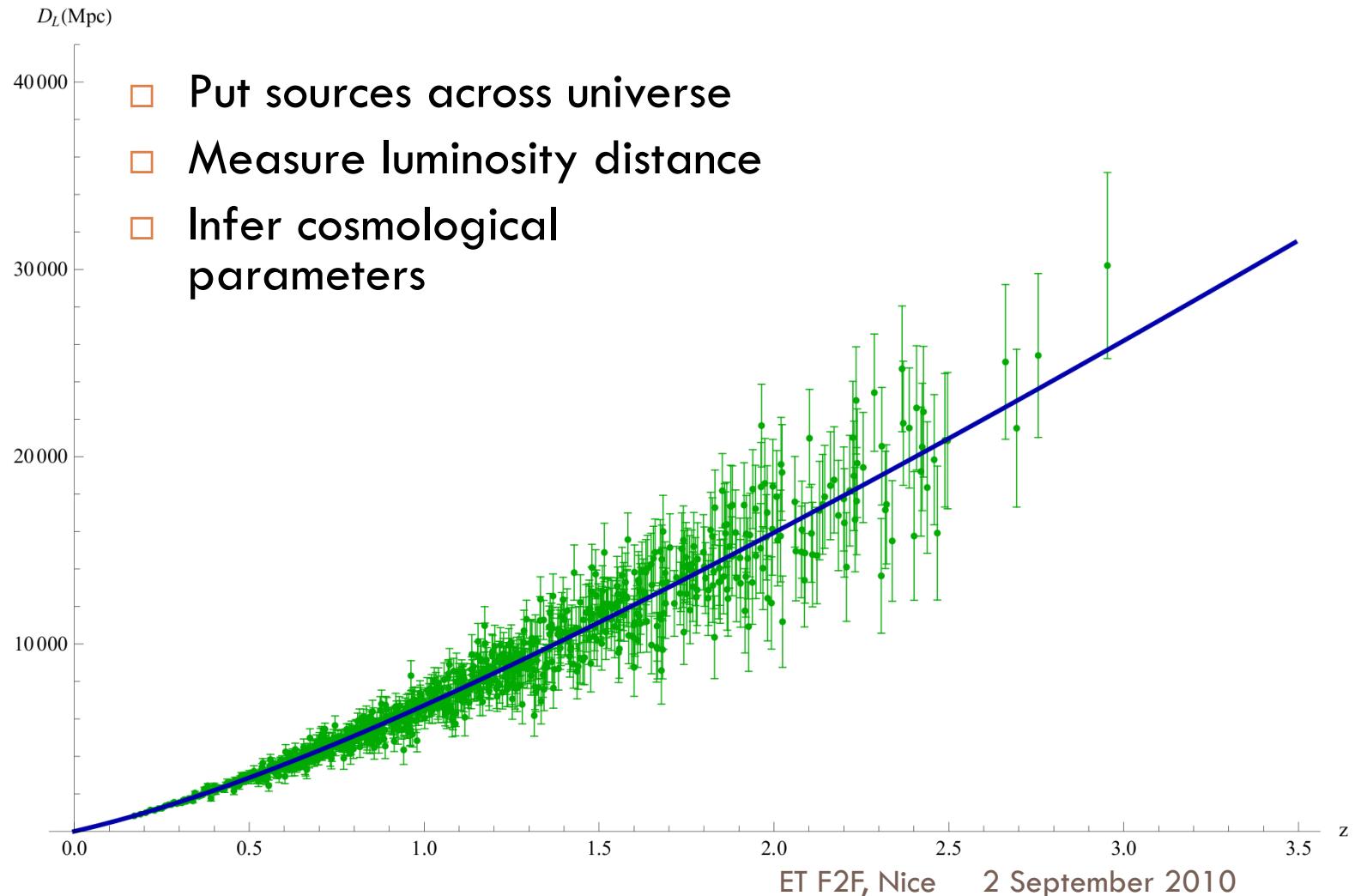
Cosmology

- Infer characteristics of the universe
  - GW signal carries information about content of the universe between source and observer
  - Information encoded in the luminosity distance
$$d_L = d_L(z; \Omega_M, \Omega_\Lambda, \Omega_k, w_0, w_a)$$
- Measure set of parameters
  - $\Omega_i$  densities
  - $w_i$  dark energy equation of state

# Measure cosmological parameters

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Cosmology



# Trade Study

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Cosmology

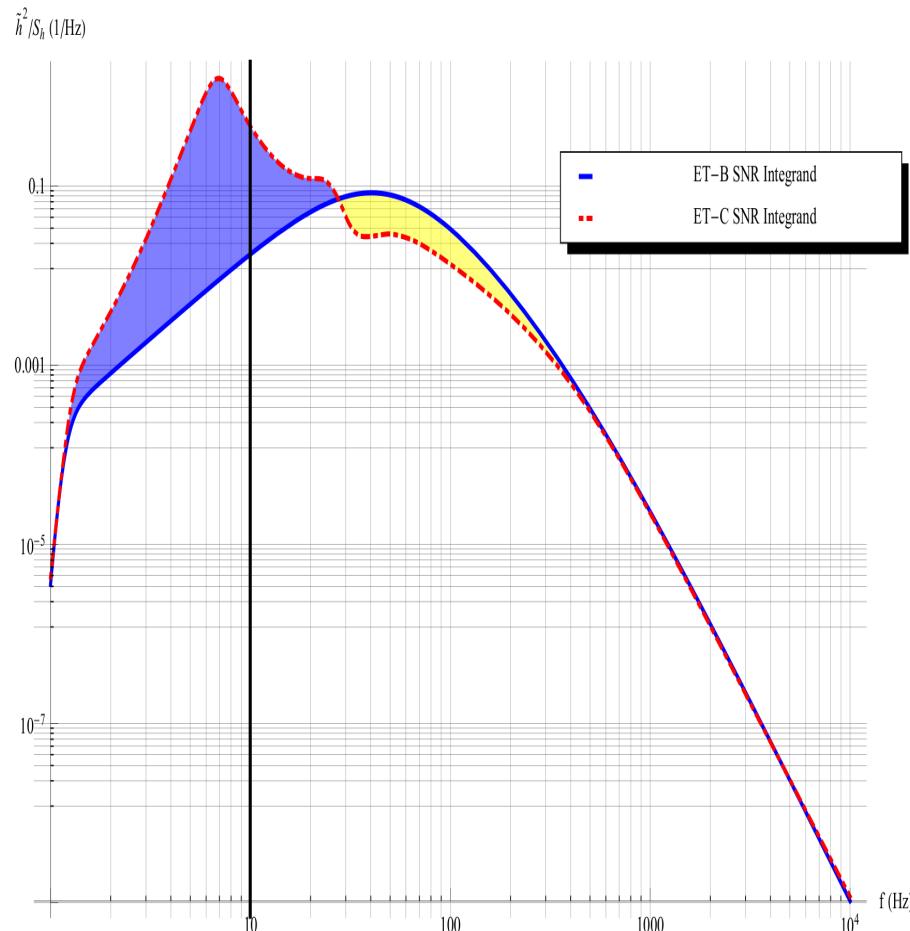
Model	$\Omega_M$	$\Omega_{DE}$	$\Omega_k$	$w_0$	$w_1$
$\Omega_M, \Omega_{DE}, \Omega_k, w_0, w_1$	1.215	1.005	1.049	1.050	1.057
$\Omega_M, \Omega_{DE}, \Omega_k$	1.298	1.207	1.228	—	—
$\Omega_M, \Omega_{DE}, w_0, w_1$	1.104	1.096	—	1.186	1.207
$\Omega_M, \Omega_{DE}, w_0$	1.162	1.162	—	1.164	—
$\Omega_M, \Omega_{DE}$	1.178	1.178	—	—	—
$w_0, w_1$	—	—	—	1.158	1.183
$w_0$	—	—	—	1.151	-
Average relative improvement:	—15.11%				

- Ratio of root mean square errors (ET-C/ET-B)
- Lower cut-off frequency 10Hz

# Discussion

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Cosmology



- Advantage of ET-C comes in at lower frequencies
  - At 10Hz, higher SNR for ET-B due to better sensitivity for >30Hz
  - Need to go below 10Hz to gain full potential of ET-C

# Conclusions

Model	$\Omega_M$	$\Omega_{DE}$	$\Omega_k$	$w_0$	$w_1$
$\Omega_M, \Omega_{DE}, \Omega_k, w_0, w_1$	1.215	1.005	1.049	1.050	1.057
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$w_0, w_1$	—	—	—	1.158	1.183
$w_0$	—	—	—	1.151	—
Average relative improvement:	<b>-15.11%</b>				
Model	$\Omega_M$	$\Omega_{DE}$	$\Omega_k$	$w_0$	$w_1$
$\Omega_M, \Omega_{DE}, \Omega_k, w_0, w_1$	0.813	0.992	0.967	0.923	0.989
$\Omega_M, \Omega_{DE}, \Omega_k$	0.777	0.826	0.810	—	—
$\Omega_M, \Omega_{DE}, w_0, w_1$	0.877	0.884	—	0.828	0.833
$\Omega_M, \Omega_{DE}, w_0$	0.815	0.815	—	0.830	—
$\Omega_M, \Omega_{DE}$	0.849	0.849	—	—	—
$w_0, w_1$	—	—	—	0.858	0.842
$w_0$	—	—	—	0.863	—
Average relative improvement:	<b>13.75%</b>				
Model	$\Omega_M$	$\Omega_{DE}$	$\Omega_k$	$w_0$	$w_1$
$\Omega_M, \Omega_{DE}, \Omega_k, w_0, w_1$	0.805	0.993	0.967	0.914	0.969
$\Omega_M, \Omega_{DE}, \Omega_k$	0.765	0.816	0.799	—	—
$\Omega_M, \Omega_{DE}, w_0, w_1$	0.872	0.879	—	0.821	0.820
$\Omega_M, \Omega_{DE}, w_0$	0.804	0.804	—	0.819	—
$\Omega_M, \Omega_{DE}$	0.838	0.838	—	—	—
$w_0, w_1$	—	—	—	0.850	0.834
$w_0$	—	—	—	0.854	—
Average relative improvement:	<b>14.66%</b>				

10Hz

5Hz

1Hz

- Parameter estimation lower cut-off frequency
- 10Hz not sufficient to probe full extend of ET-C
- Only if  $f_{\text{low}} \sim 5\text{Hz}$ , will ET-C be beneficial for parameter estimation

# Testing General Relativity

Checking consistency between post-Newtonian  
phase coefficients

# Post Newtonian Formalism

- General form of waveforms in Post-Newtonian (PN) formalism

- Both amplitude and phase expanded in  $v/c$

$$h(t; \vec{\theta}) = \sum_{n=1}^{N_H} \sum_{k=0}^K A_{nk}(t) \cos(n\Phi(t) + \phi_{nk})$$

- Phase evolution represented as

$$\Phi(t) = \phi_c - \sum_{l=0}^L \phi_l (t_c - t)^{(5-l)/8} \quad \text{where} \quad \phi_l = \phi_l(m1, m2)$$

- Similar in frequency domain (e.g. SPA)

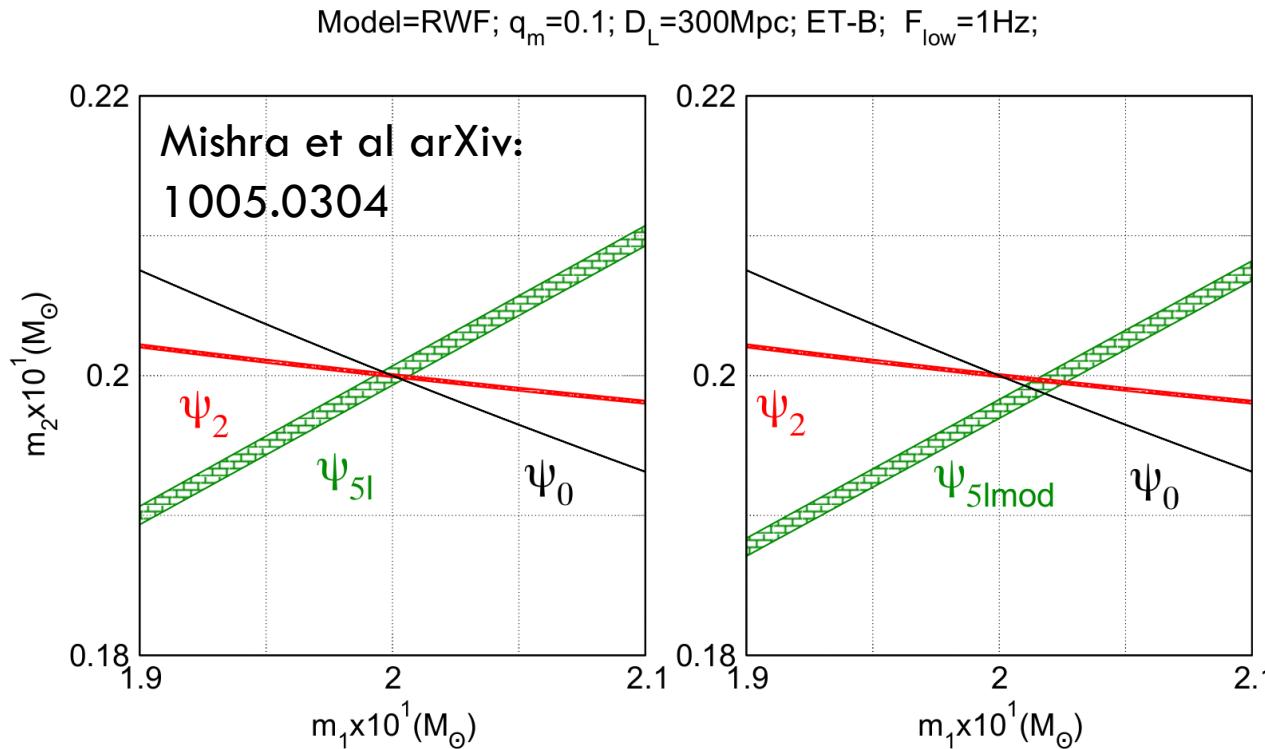
$$h(f; \vec{\theta}) = A(f) e^{i\Psi(f)} \quad \Psi(f) = 2\pi f t_c - \phi_c + \sum_{l=0}^L \psi_l f^{(l-5)/3}$$

# Testing General Relativity: Concept

Arun et al. 2006

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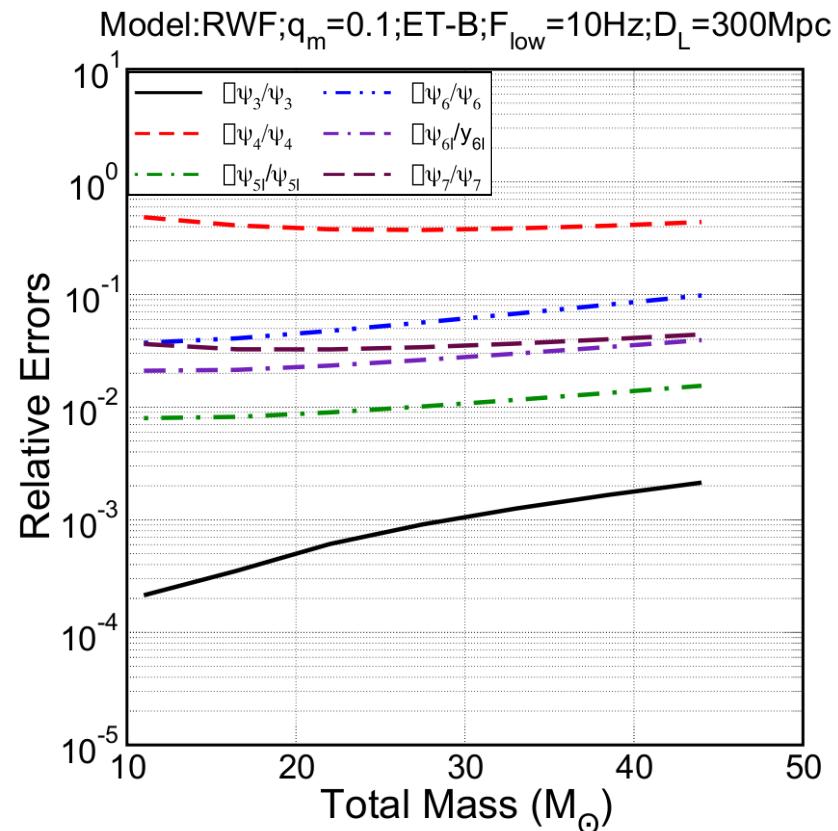
Testing General Relativity



- In GR, only two phase coefficients independent
- Assume spinless systems

- Measure  $\phi_0, \phi_2, \phi_T$  independently
- Check for consistency between PN phase coefficients

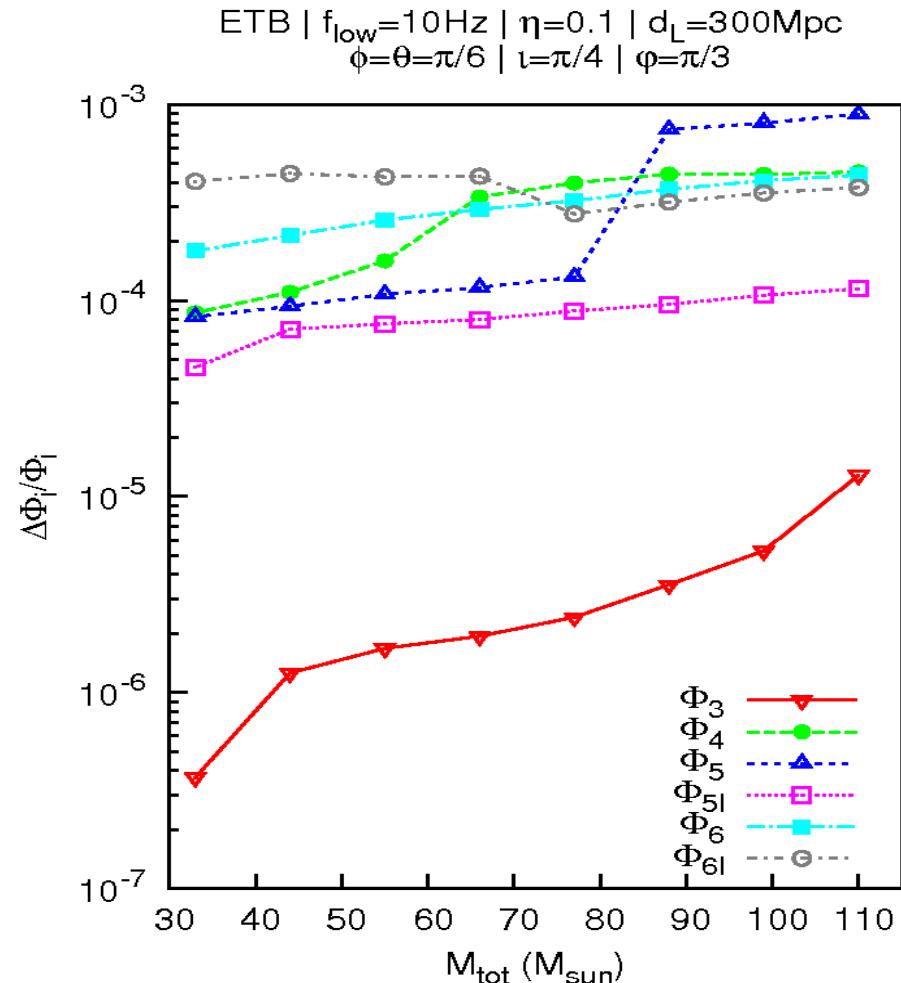
- Proposed test explored in frequency domain
  - Using SPA waveforms
  - ETB shown
- Shows validity of scheme
  - Errors for  $\psi_3 \sim 0.01\%$
  - Greater errors for  $\psi_k$ ,  $k > 3$  (1%-100%)



Mishra et al arXiv:1005.0304

# Time Domain Coefficients

- Similar can be done for time domain phase coefficients
  - ▣  $\phi_i$  instead of  $\psi_i$
- Time domain parameterisation shows better performance
  - ▣  $\sim 50x$  better relative sensitivity
  - ▣ Yet to understand in full detail

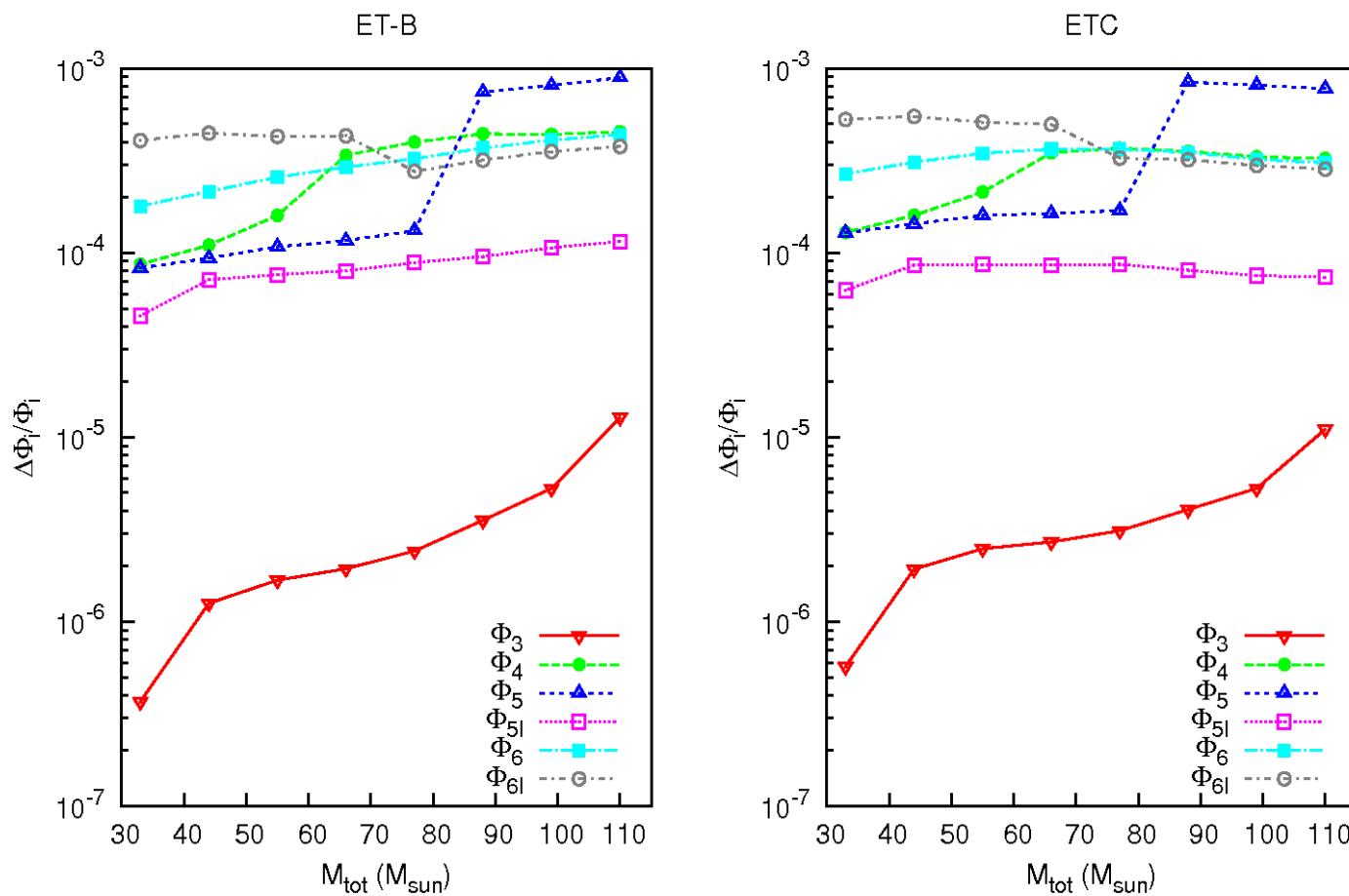


# Trade Study

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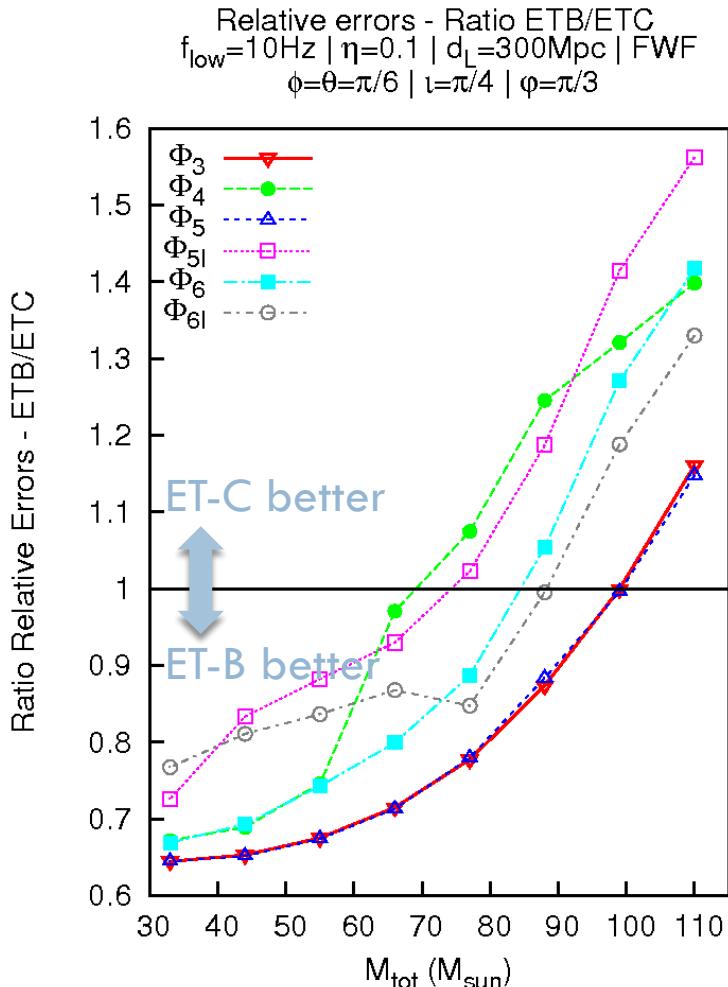
Testing General Relativity

Relative errors PN phase coefficients  
( $f_{\text{low}}=10\text{Hz}$  |  $\eta=0.1$  |  $d_L=300\text{Mpc}$  | FWF |  $\phi=\theta=\pi/6$  |  $\iota=\pi/4$  |  $\varphi=\pi/3$ )



ET F2F, Nice    2 September 2010

# Discussion



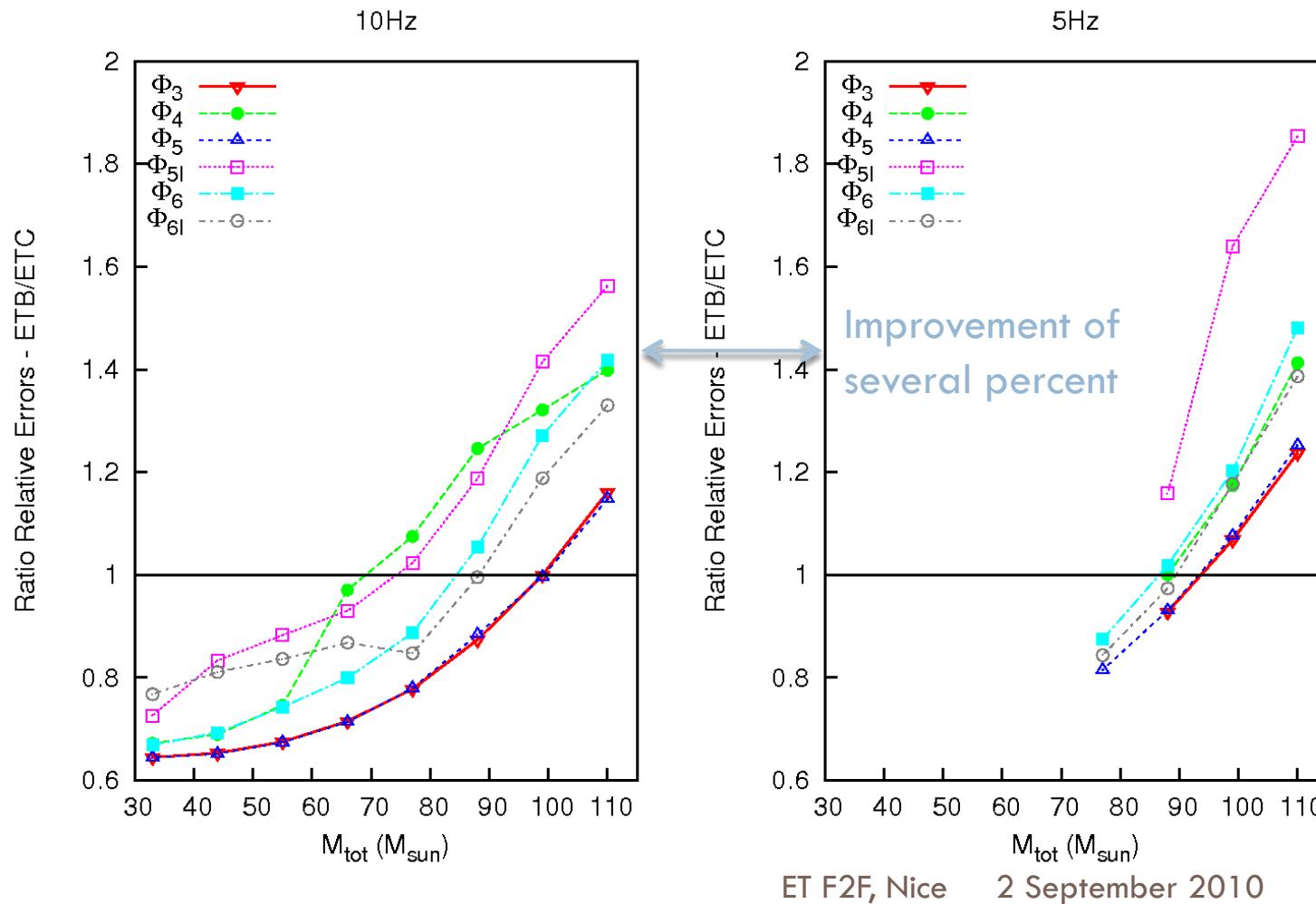
- ET-C performs better than ET-B in the high mass region
  - $F_{\text{ISO}}$  decreases with mass
- Difference as large as 40%
- Transition around 70-90  $M_{\odot}$



Best performance depends on the sources of interest

# Discussion 2

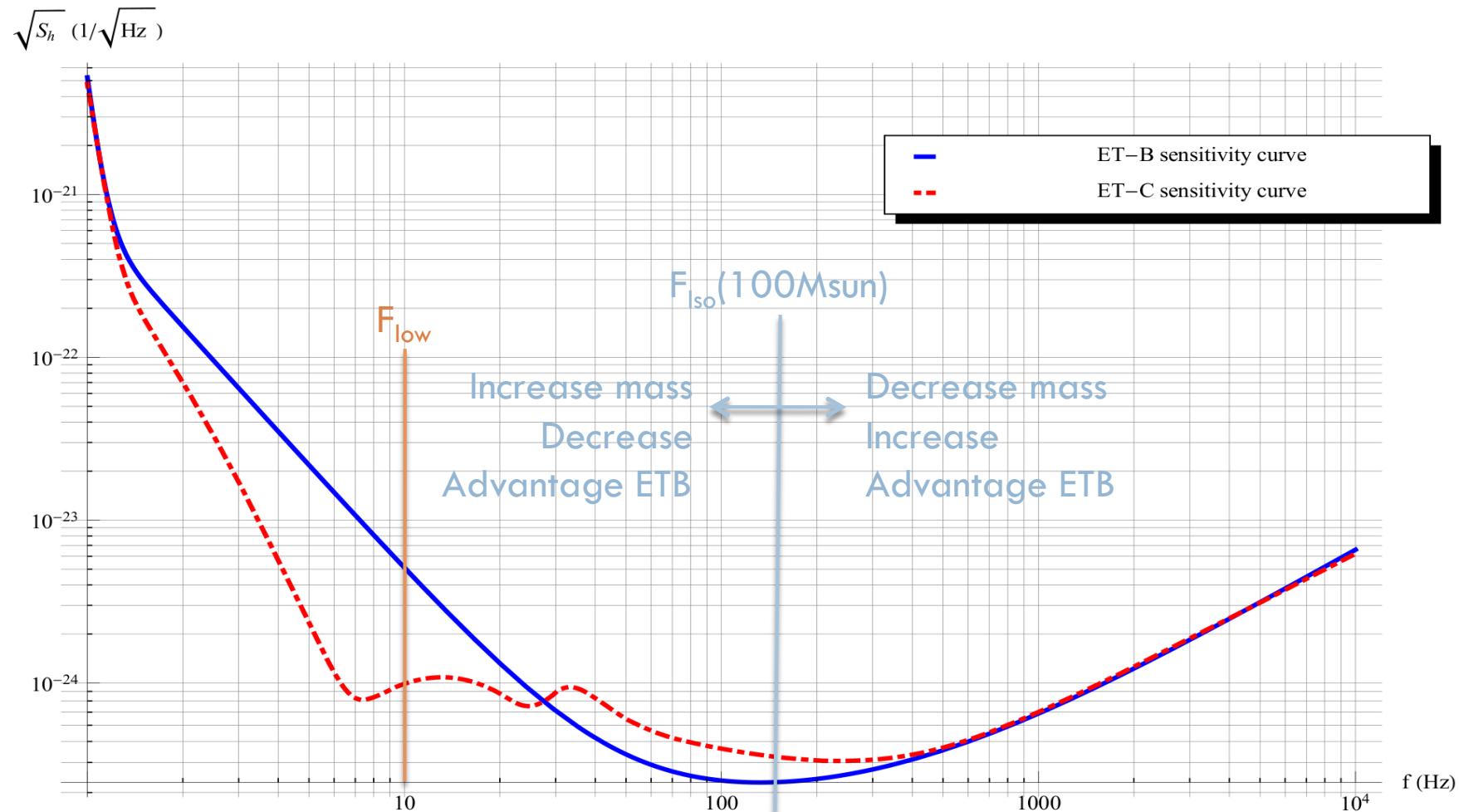
Comparing lower cut-off frequencies



# Discussion 3

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Testing General Relativity



- Cosmology doesn't benefit from ET-C if lower cut-off is set to 10Hz
- Testing General Relativity only benefits at high total mass systems
- All can be attributed to sensitivity loss between 30Hz-500Hz



**Full benefits of ET-C are only used if the lower cut-off frequency can be pushed down to below 10Hz**

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# Backup Slides

If the talk did not provide sufficient detail